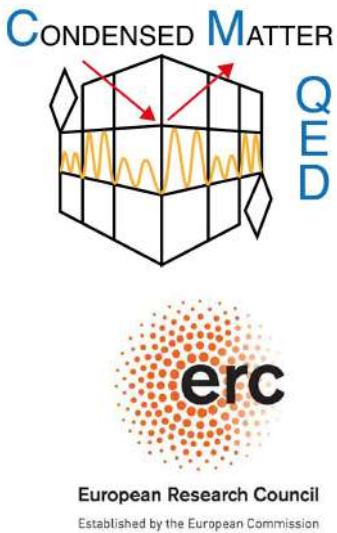
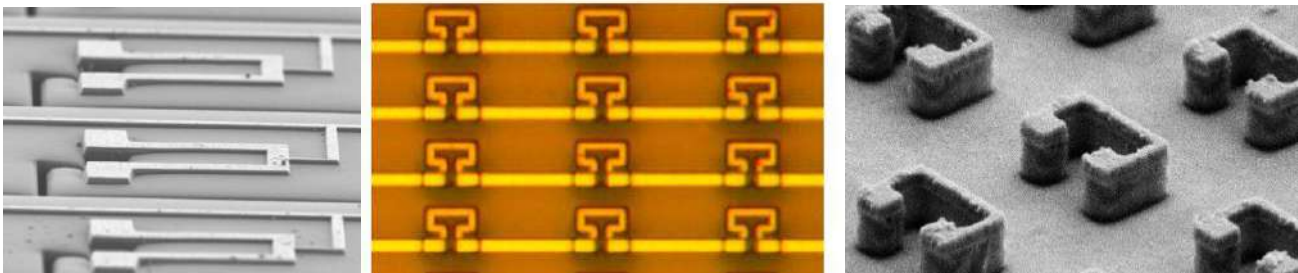




Cavities and metamaterials for infrared optoelectronics: fundamental studies and applications

Yanko Todorov

Laboratoire de Physique et d'Étude des Matériaux (LPEM)
ESPCI, Université PSL, CNRS, Sorbonne Université, Paris, France



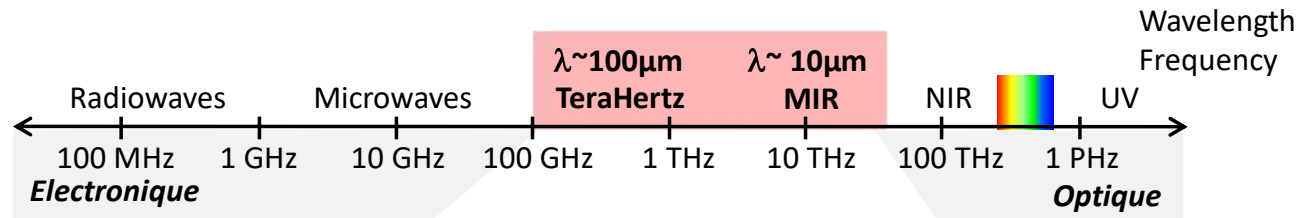
Summary

1. Introduction
2. Patch antenna cavities and their applications
3. THz “meta-atoms”

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3. THz “meta-atoms”

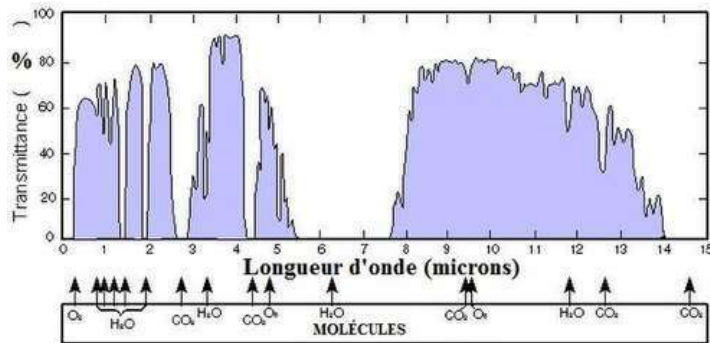
Where am I?



Very wide frequency range, with many applications:

- Thermal imaging
- Non-invasive spectroscopy
- Molecular spectroscopy
- Free space communications

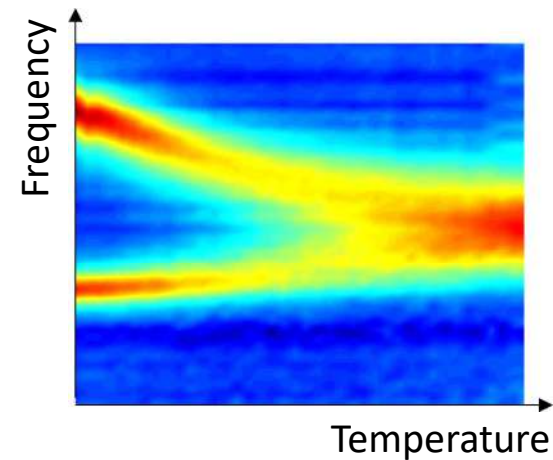
-...



Source: Wikipedia

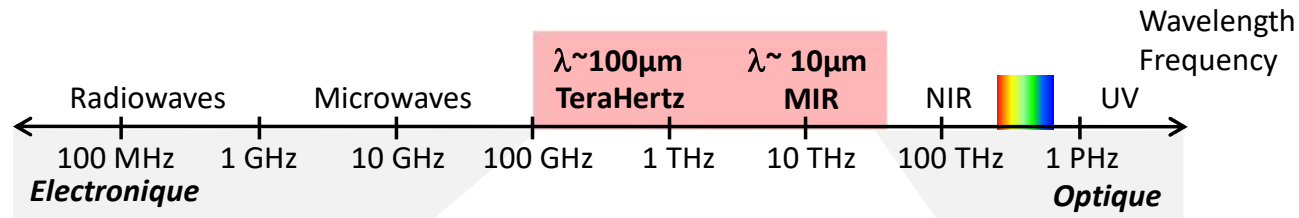
...and playground for fundamental studies

-Ultra-strong light-matter coupling regime



Todorov *et al.* PRL **102**,186402 (2009)

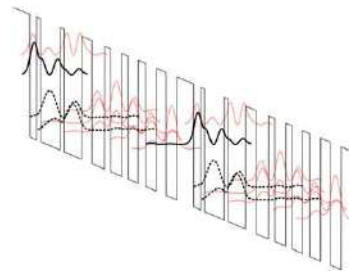
Infrared opto-electronics



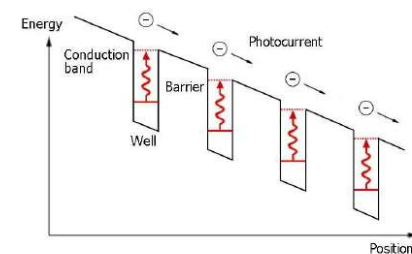
Many technologies to generate & detect such wavelengths:

- Unipolar devices
- Colloidal crystals & MCT
- Type II heterostructures
- Nonlinear conversion
- Gas lasers
- Electronic oscillators (multipliers)
- Bolometers
- Graphene based devices...

- Quantum cascade laser (J. Faist, Bell Labs, 1994)

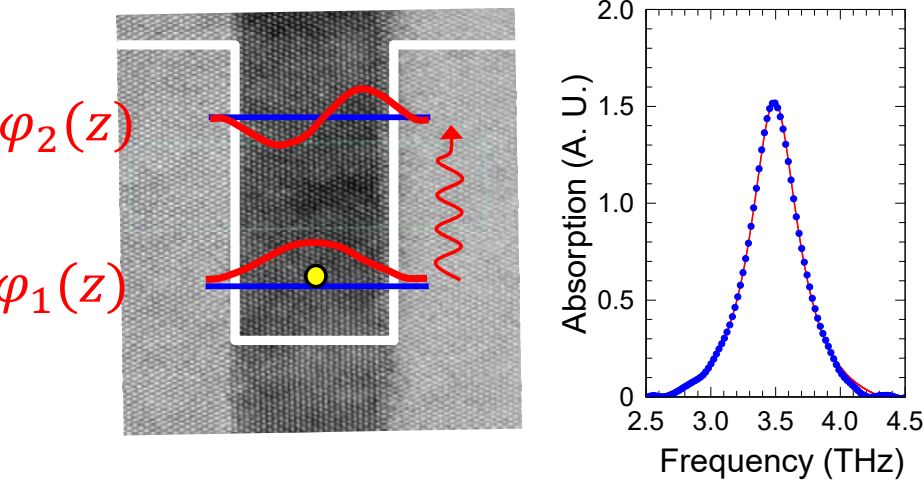


- Quantum well detectors (B. F. Levine, Bell Labs, 1987)

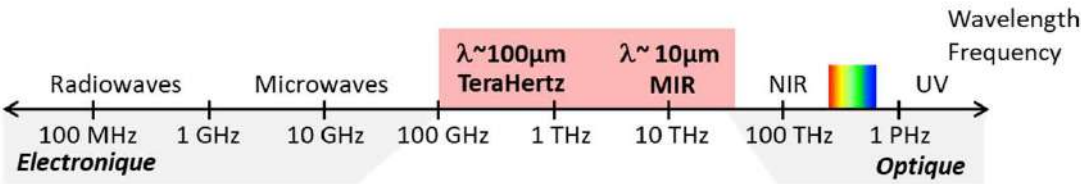


Semiconductor Quantum Well: basic building block

Quantum wells: artificial 1D potentials for electrons

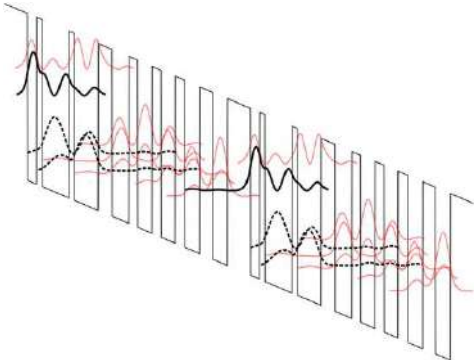
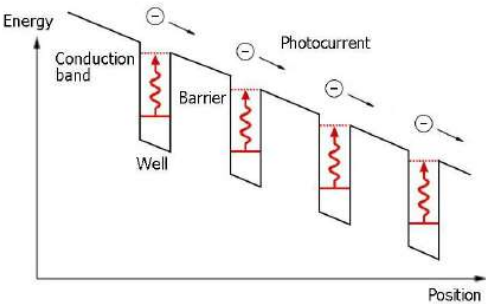


- Transitions can be tuned from MIR to THz
- Design of electronic wavefunctions

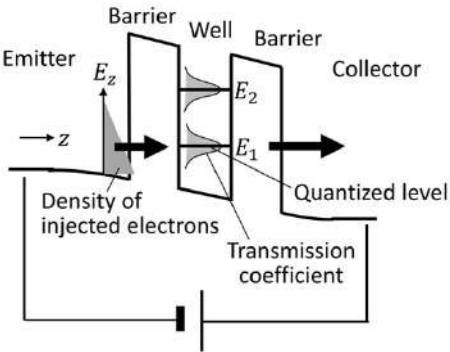
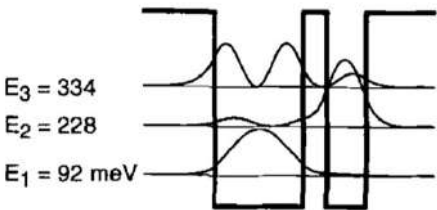


Building blocks for optoelectronic devices in the MIR & THz region

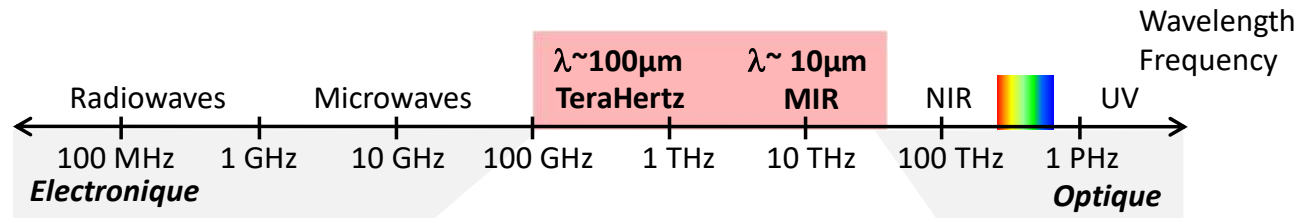
- Quantum well detectors (B. F. Levine, Bell Labs, 1987)
- Quantum cascade laser (J. Faist, Bell Labs, 1994)



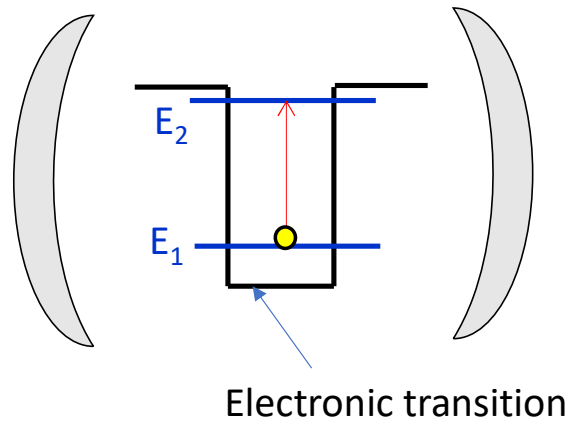
- Nonlinear optics (C. Sirtori, Bell Labs, 1994)
- Resonant-tunneling diodes



“Basic” device architecture



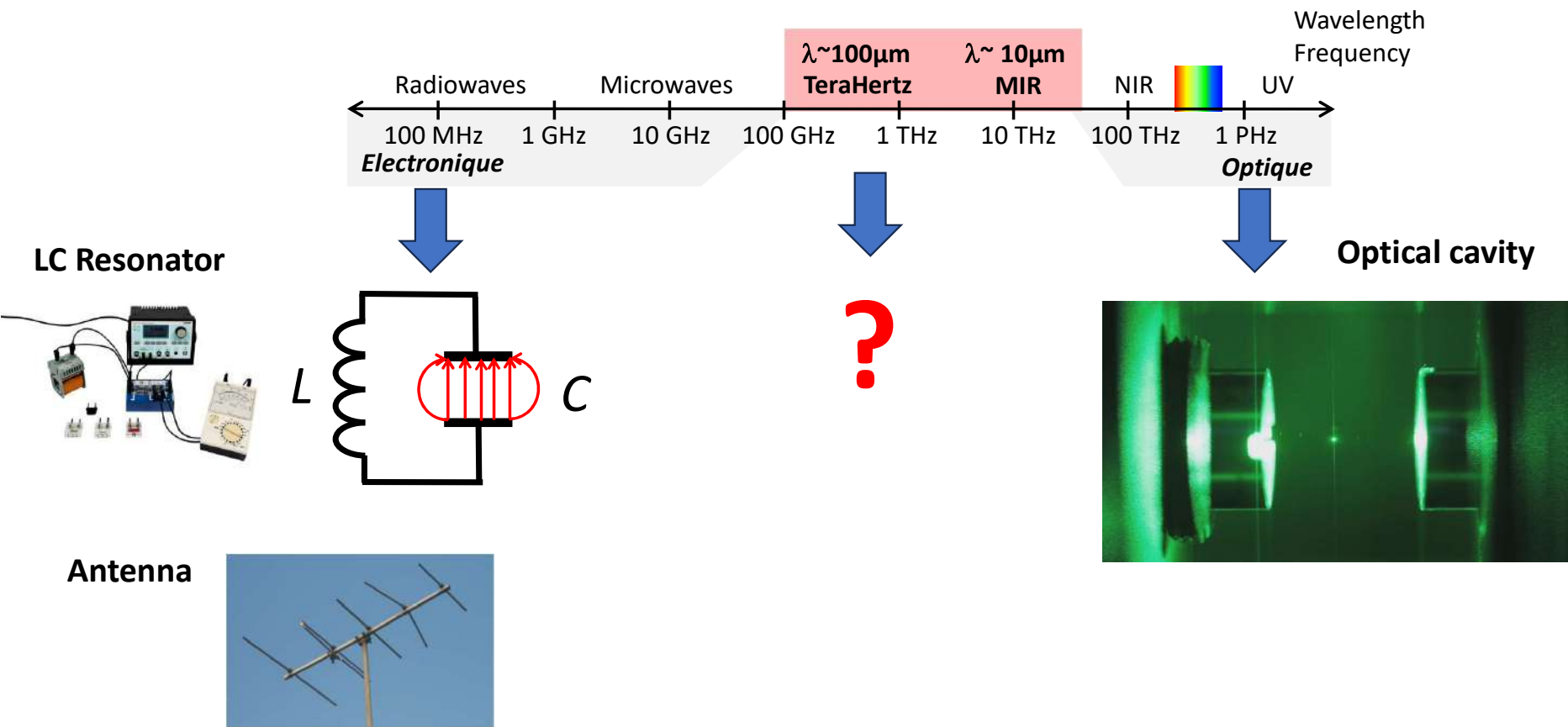
Microcavitiy



Questions (2000s-2010s):

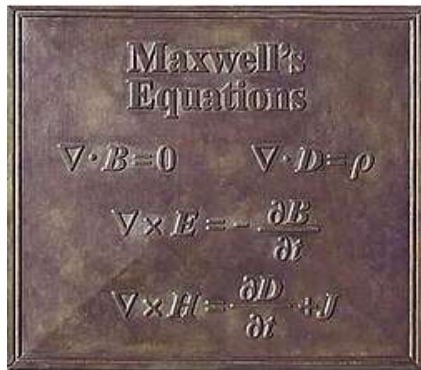
- What kind of “microcavities”?
- How to optimize the light-matter interaction in such systems?
- What problems can be solved ?

Well-known objects from electromagnetics



Sources: internet

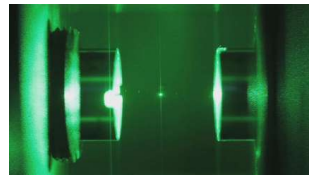
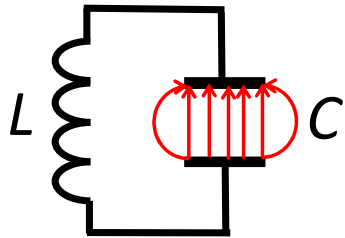
More advanced concepts



Antenna

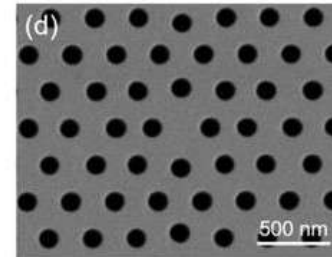


LC Resonator



Optical cavity

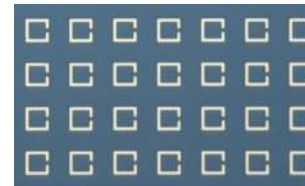
Photonic crystals: E. Yablonovitch, *PRL* **58**, 2059 (1987)



(d) *Appl. Phys. Lett.* 112, 093101 (2018)

Metamaterials:

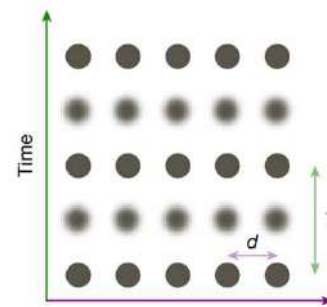
J.B. Pendry, et al., *IEEE Trans. Microwave Theory Tech.* **47**, 2075 (1999)



Bound states in the continuum (BIC):

C. W. Hsu, et al. *Nature Rev. Mat.* **1**, 16048 (2016)

Photonic Time crystals:



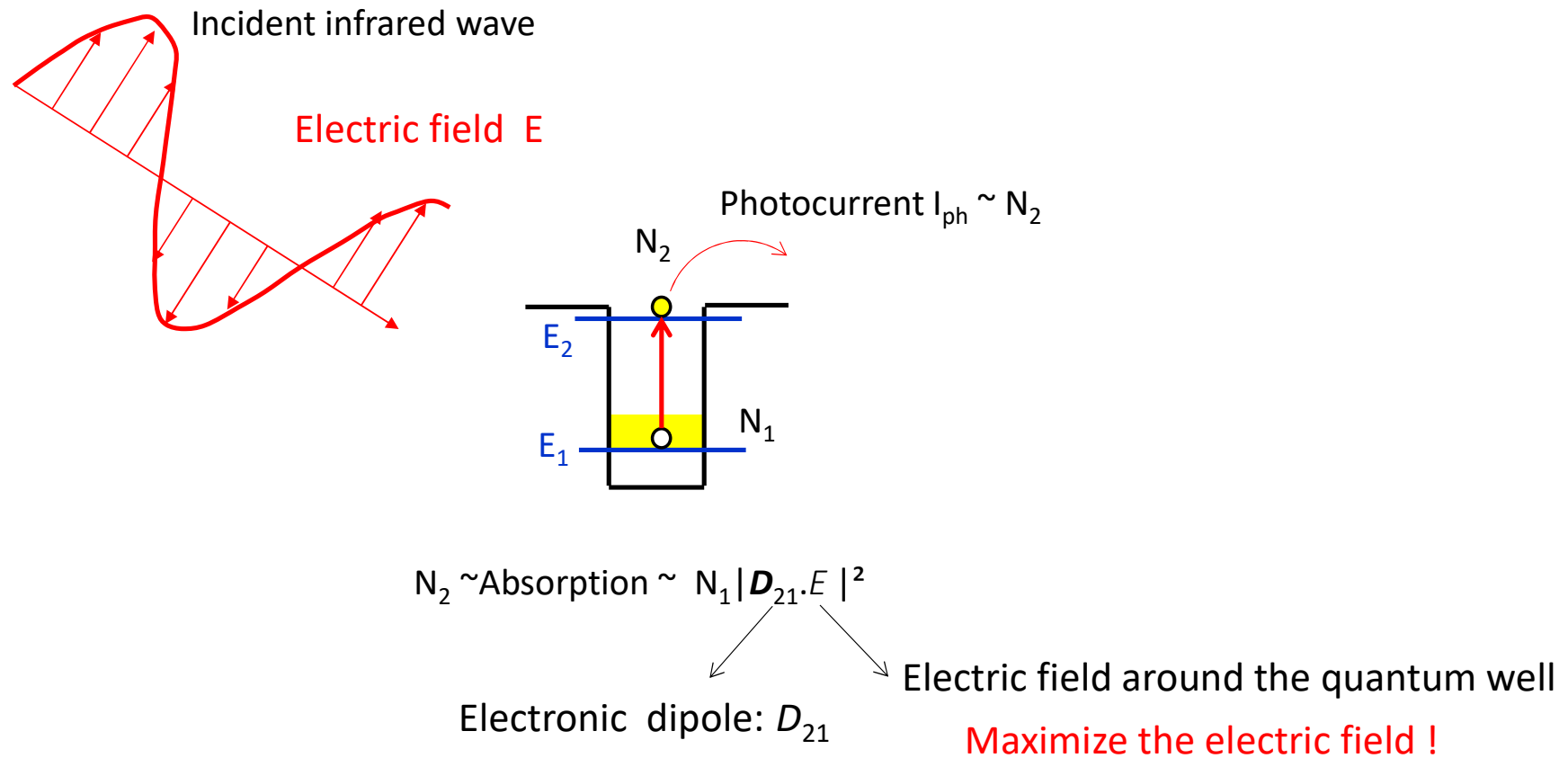
Y. Laplace & coworkers
Nature **656**, 343–348 (2026)

....

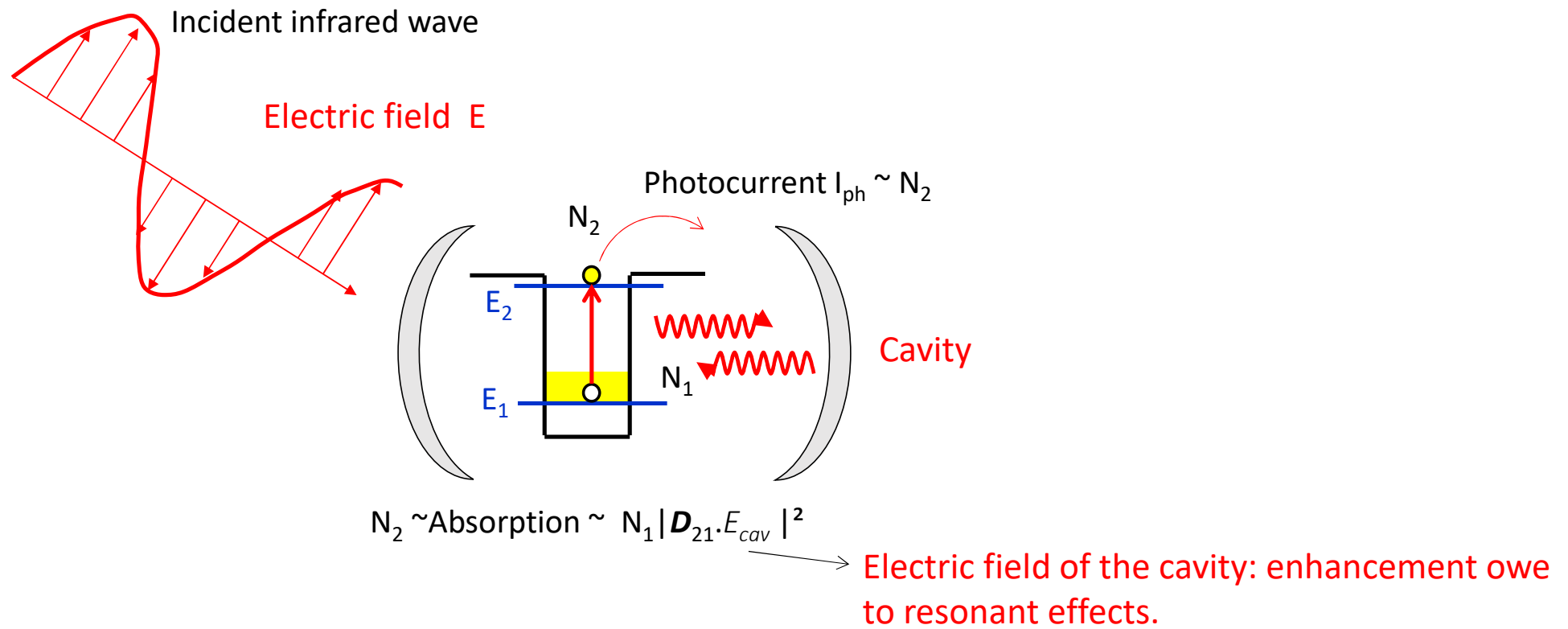
Summary

1. Introduction
2. Patch antenna cavities and their applications
3. THz “meta-atoms”

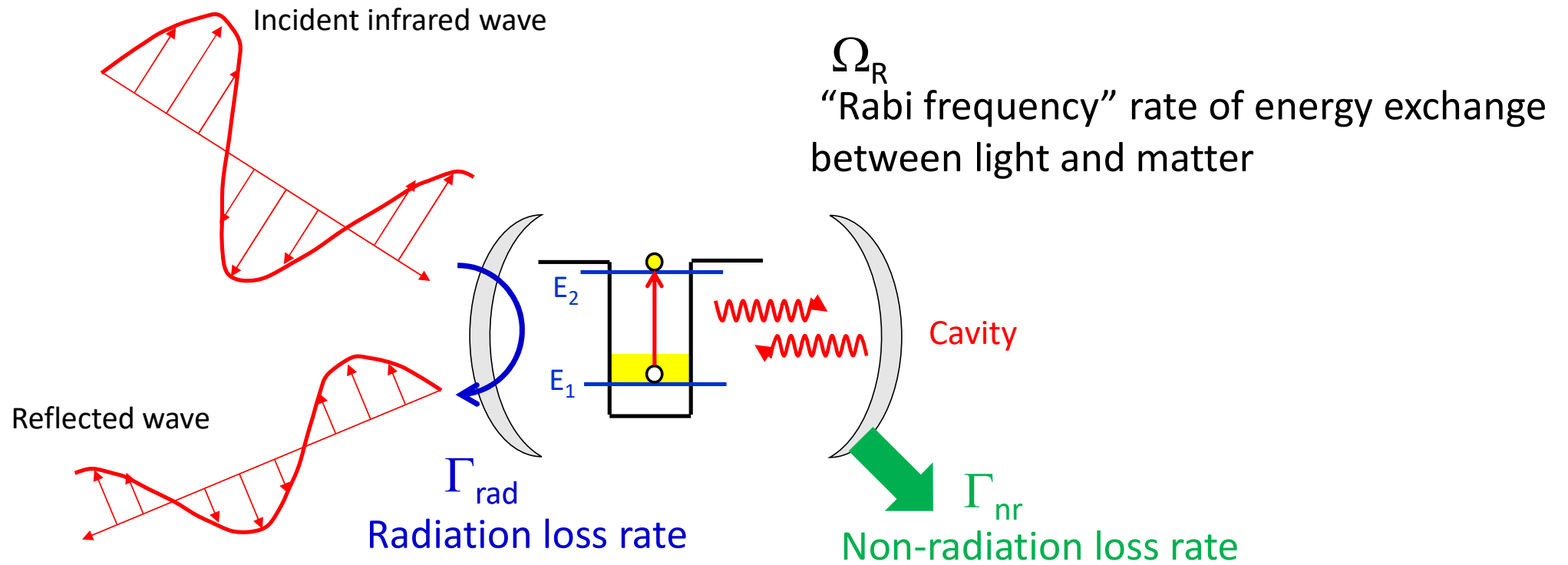
Practical example: let us consider a detector of IR waves



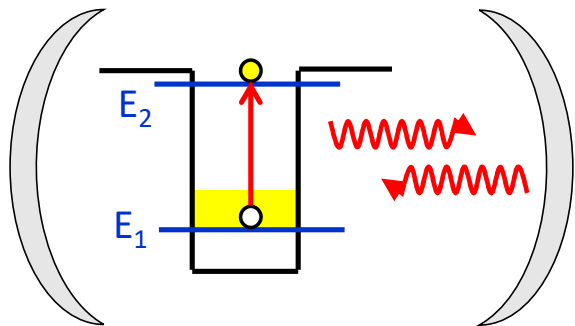
Practical example: let us consider a detector of IR waves



Important quantities



Light-matter interaction

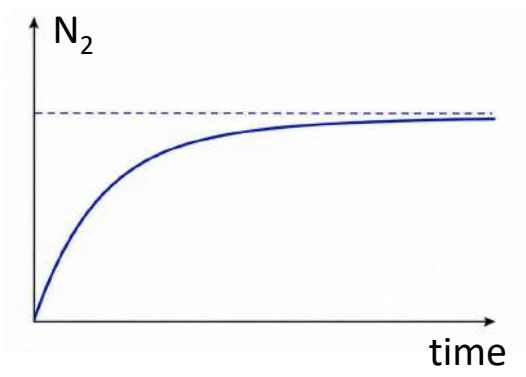


$$\Omega_R = \frac{\sqrt{N_1} D_{12} E_{vac}}{\hbar}$$

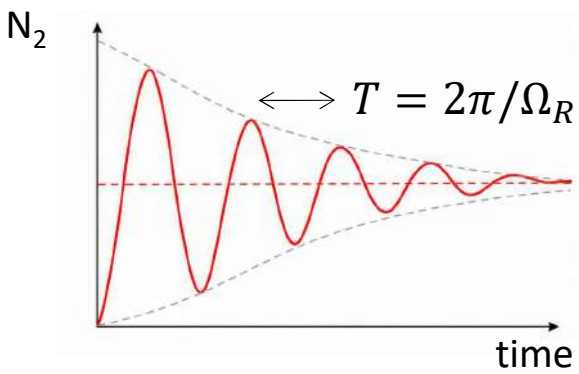
$$E_{vac} = \sqrt{\frac{\hbar \omega_{cav}}{\epsilon \epsilon_0 V_{cav}}}$$

Effective cavity volume:
Make it as small as possible!

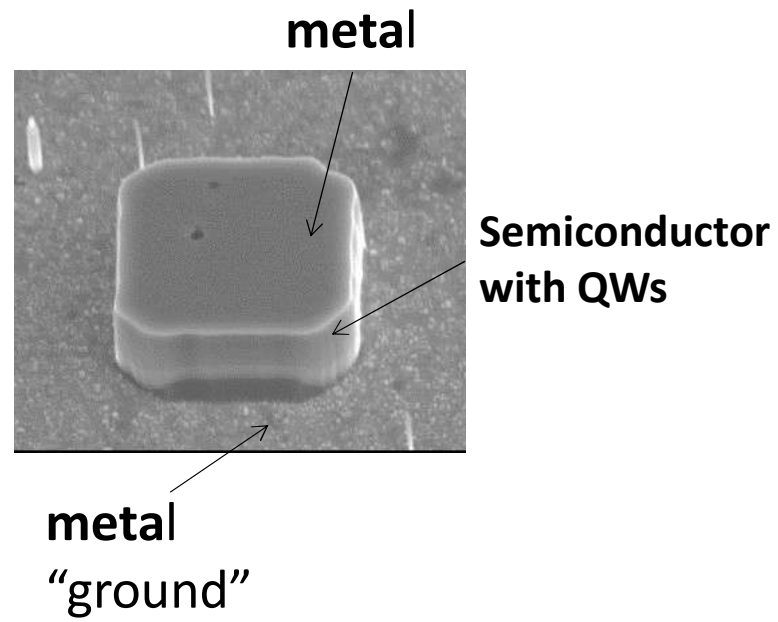
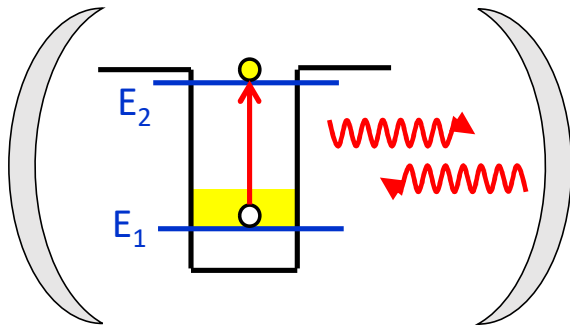
“Weak coupling”
 $\Omega_R < \Gamma_r, \Gamma_{nr}$



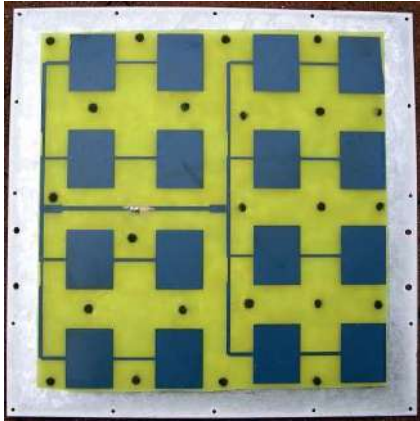
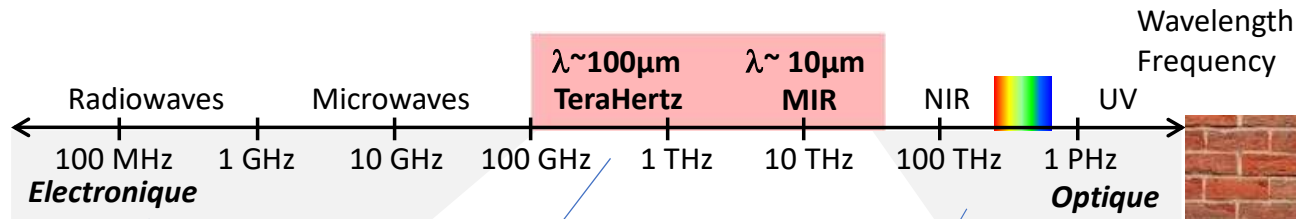
“Strong coupling”
 $\Omega_R > \Gamma_r, \Gamma_{nr}$



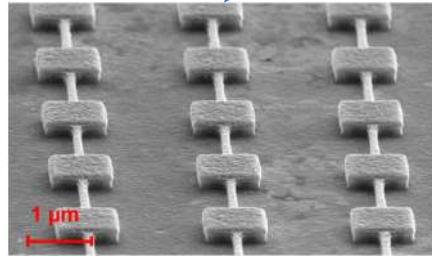
Implementation: Patch antenna cavities



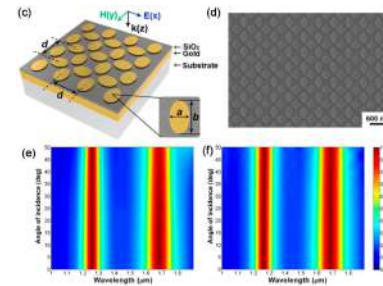
« MIMs » resonators: state of the art



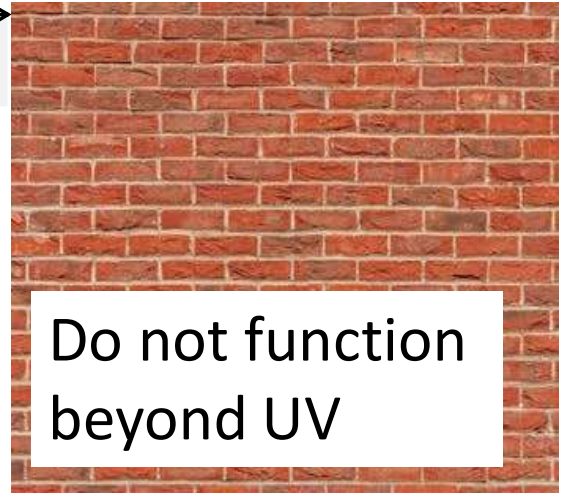
Very common microwave component
(antenna function:
receivers & emitters)



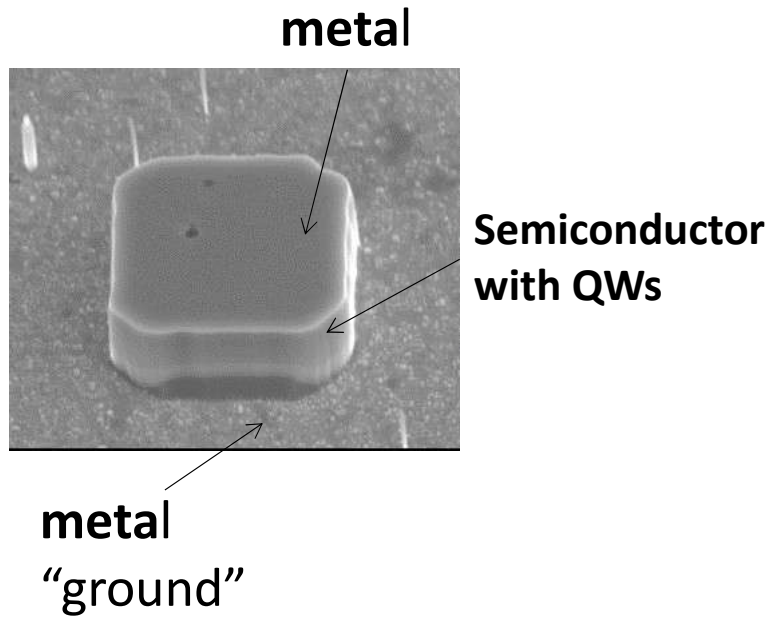
Optoelectronic applications
Fundamental studies



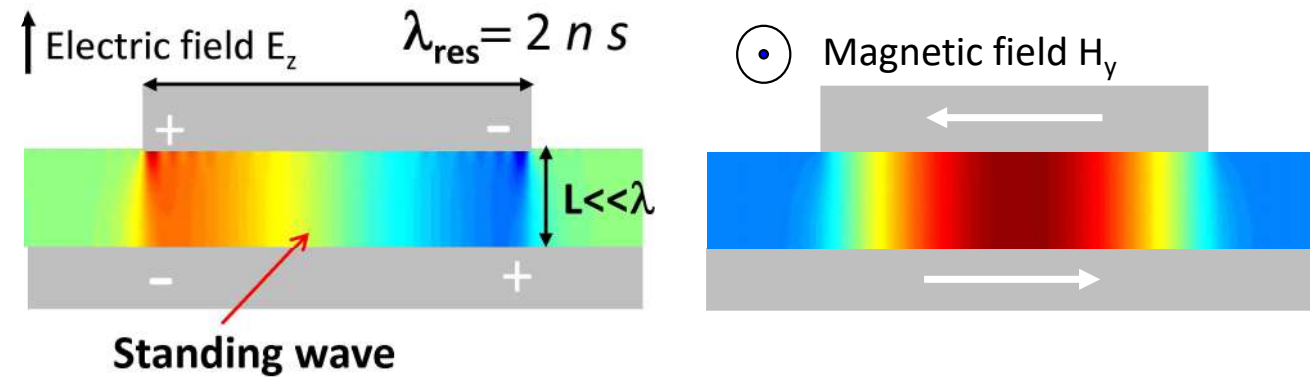
Perfect absorbers
Thermal emission
Photovoltaic devices
...



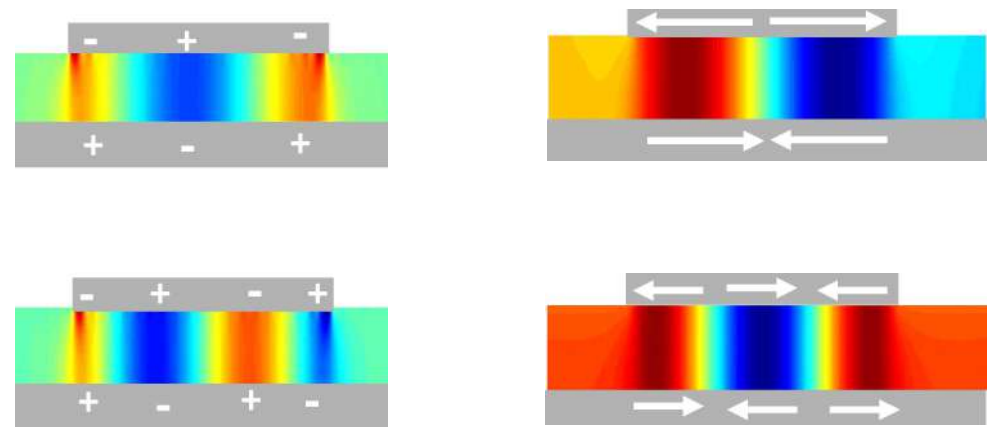
THz Patch antenna cavities



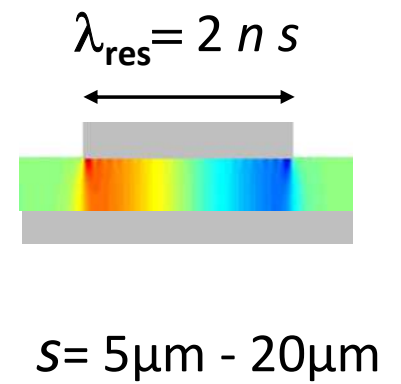
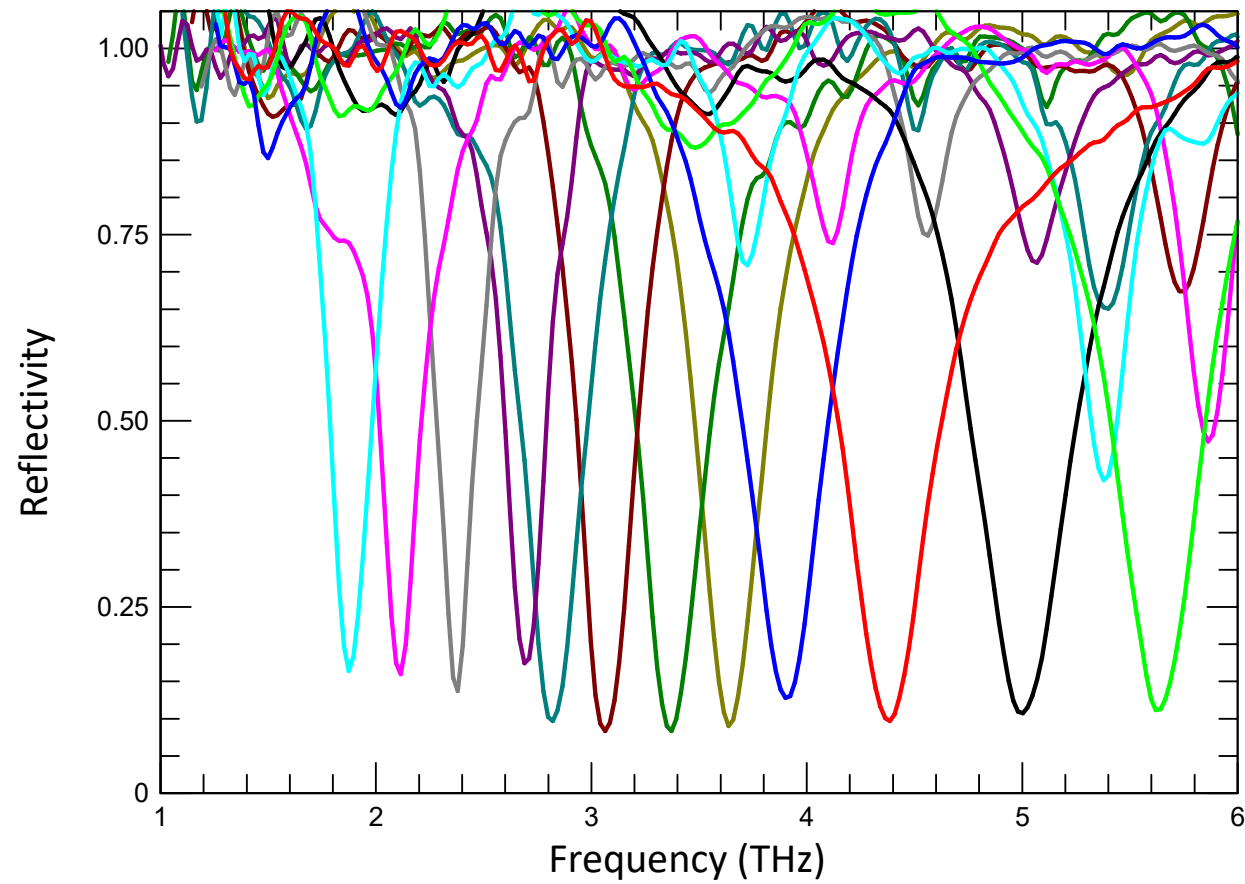
- **Fundamental mode**



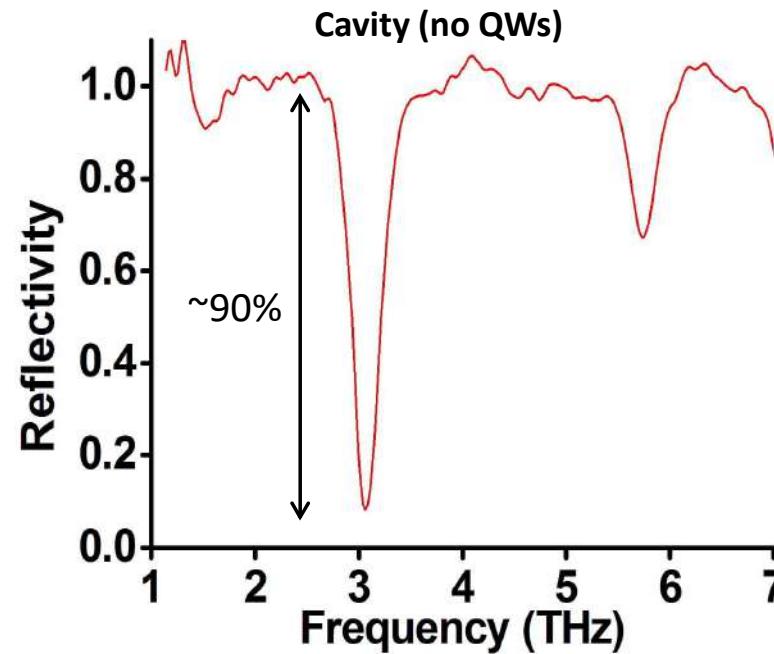
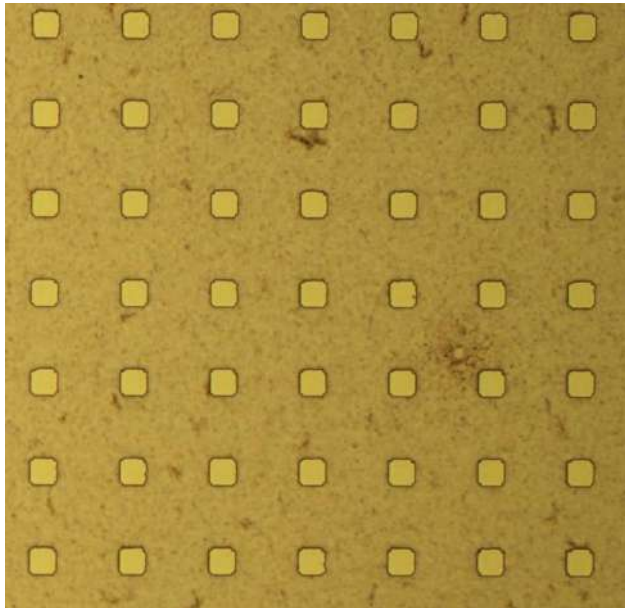
- **High order modes**



Tuning of the resonant mode



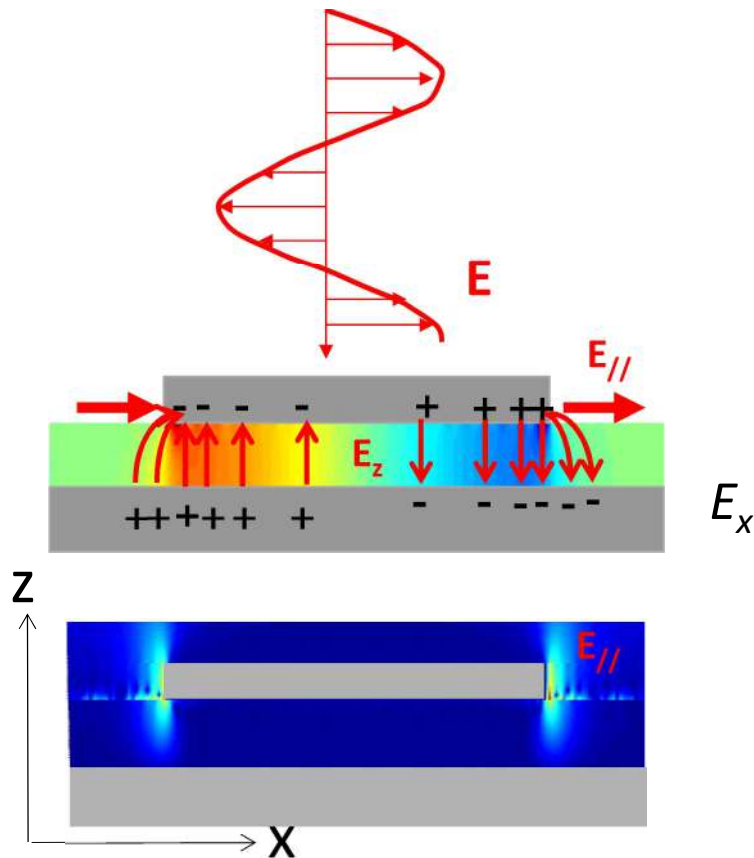
Actual experiments are performed on dense arrays ...



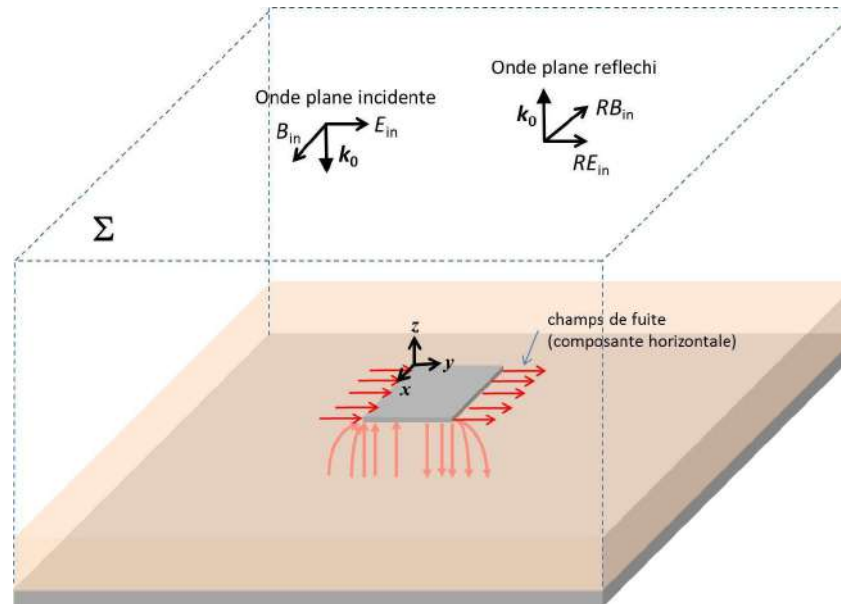
The array configuration is important
In order to increase the
free space coupling rate Γ_{rad} !

Analytical modelling of free space-coupling of the array

- Fringing field play important role



- Array unit cell



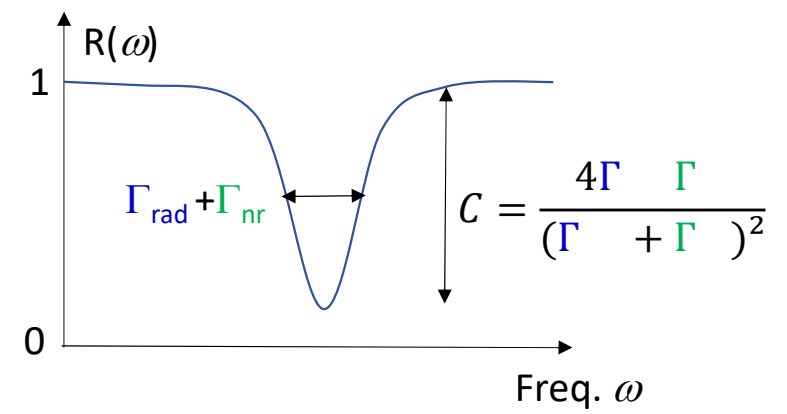
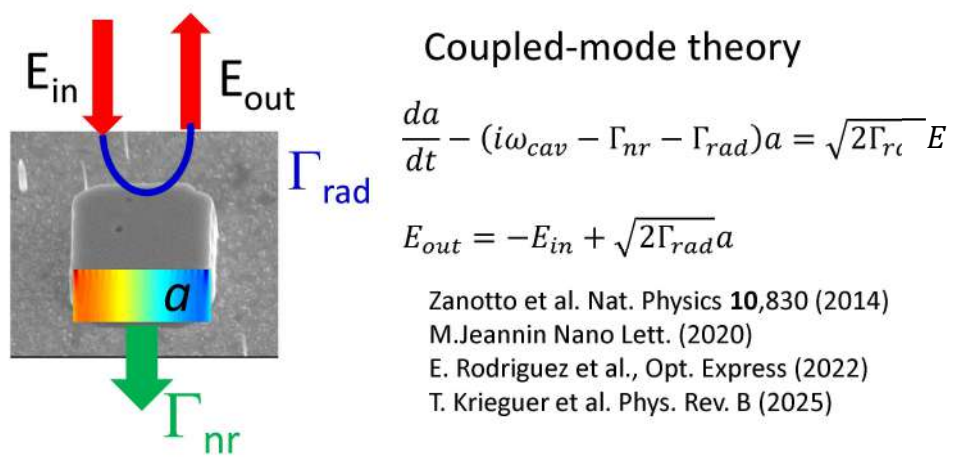
- Electric field of the incident wave is matched to the in-plane fringing fields
- Energy conservation

Radiation loss rate:

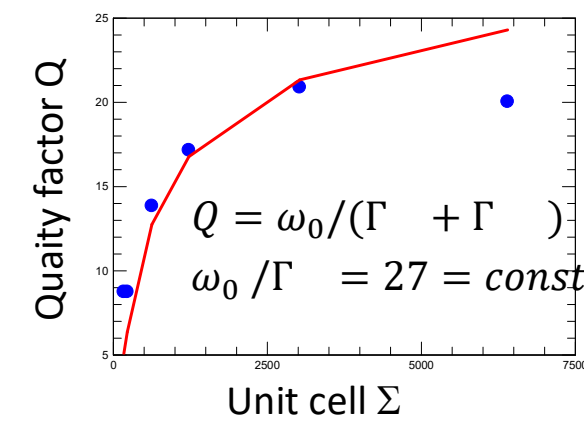
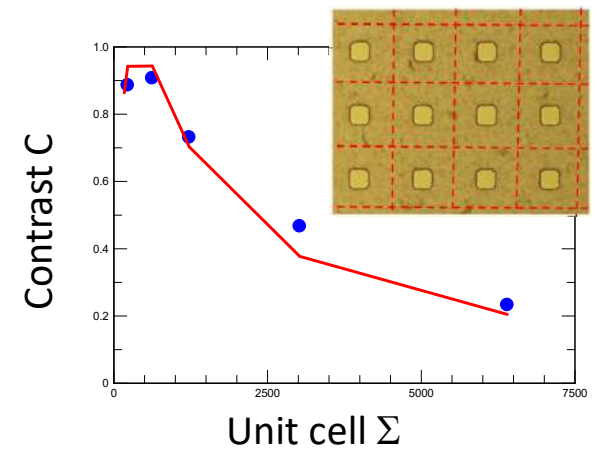
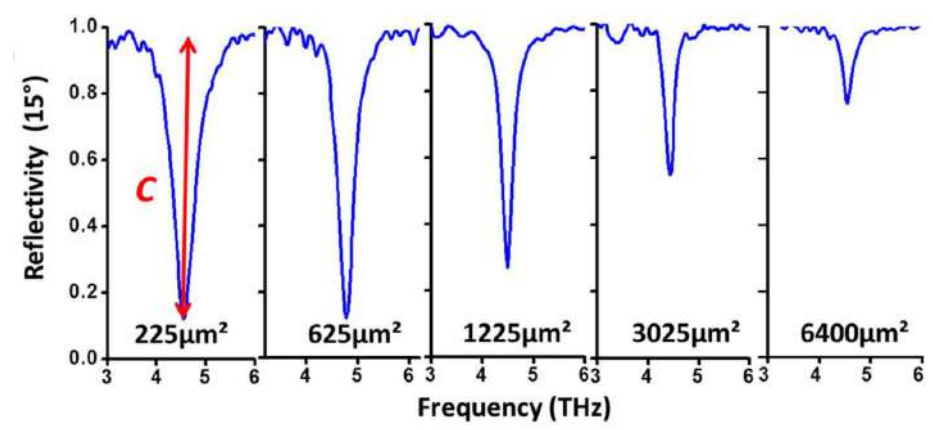
$$\Gamma_{rad} = \frac{2cL}{n^2 \Sigma}$$

C. Feuillet-Palma *et al.*, Sci. Rep. **3**, 1361 (2013)

Analytical modelling of array reflectivity

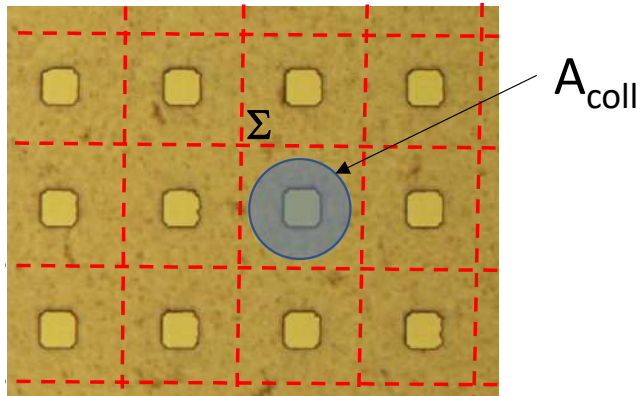
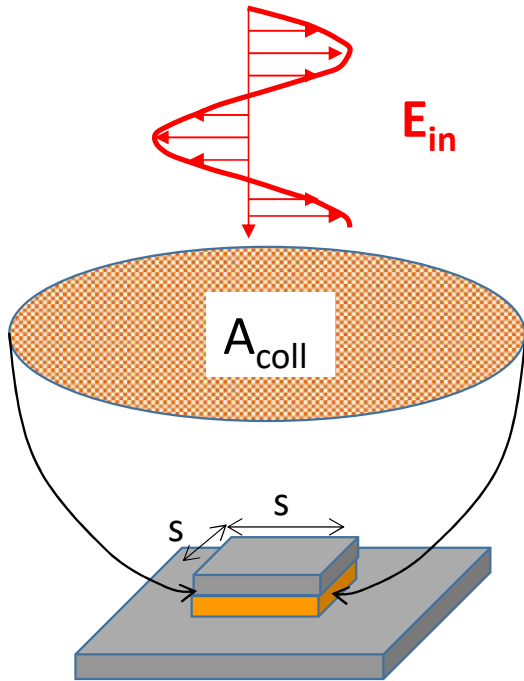


Array effects



D.Palaferri et al., New J. Phys. **18** 113016 (2016)
E. Rodriguez et al., Opt. Express (2022)

Collection area & Local field enhancement



- Collection area:

Each elements of the array
absorb on an effective area:

$$A_{\text{coll}} = C\Sigma$$

Typically, $A_{\text{coll}} \sim 10s^2$:

Antenna Effect

- Local field enhancement:

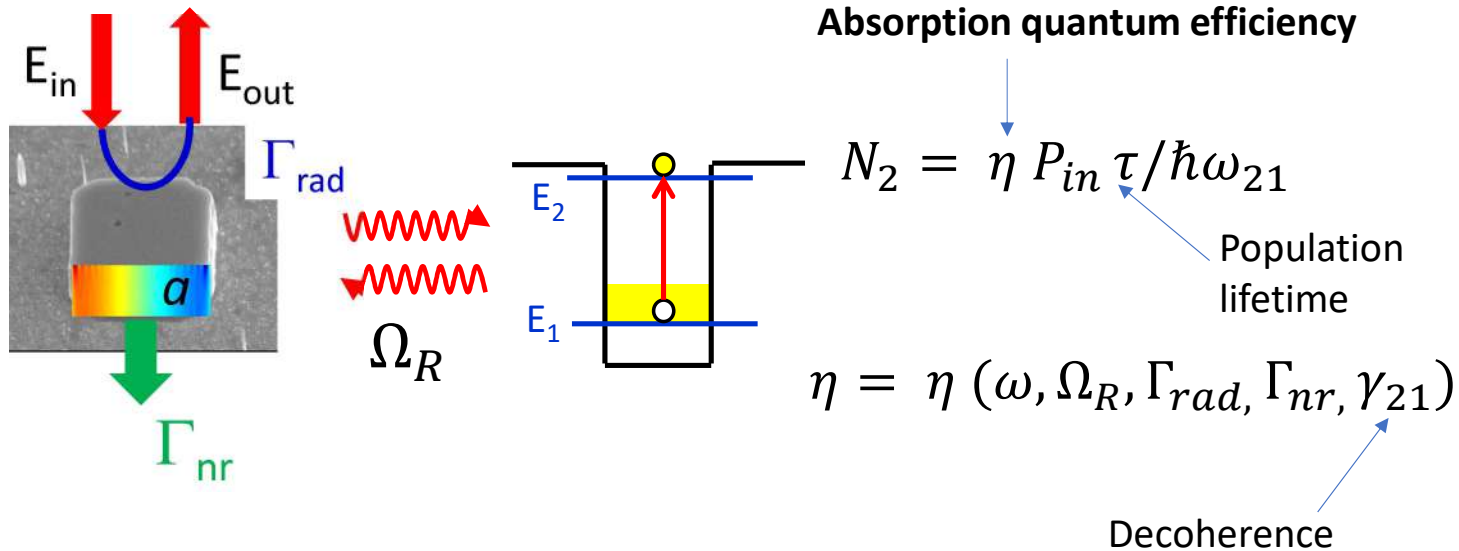
$$\frac{\varepsilon |E_0|^2}{|E_{in}|^2} = \frac{A_{\text{coll}} \lambda}{\pi V_{\text{cav}}} Q_{nr}$$

Focusing factor

$$F = \frac{A_{\text{coll}} \lambda}{V_{\text{cav}}} Q_{nr}$$

Coupling with quantum wells

Maxwell-Bloch equations (1):



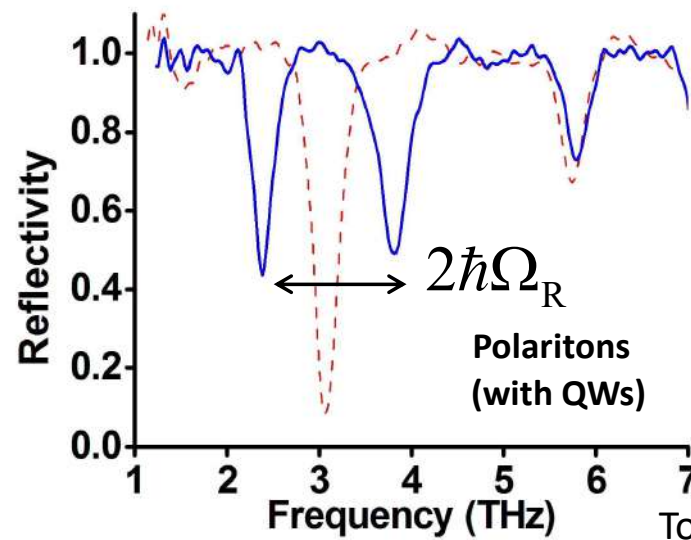
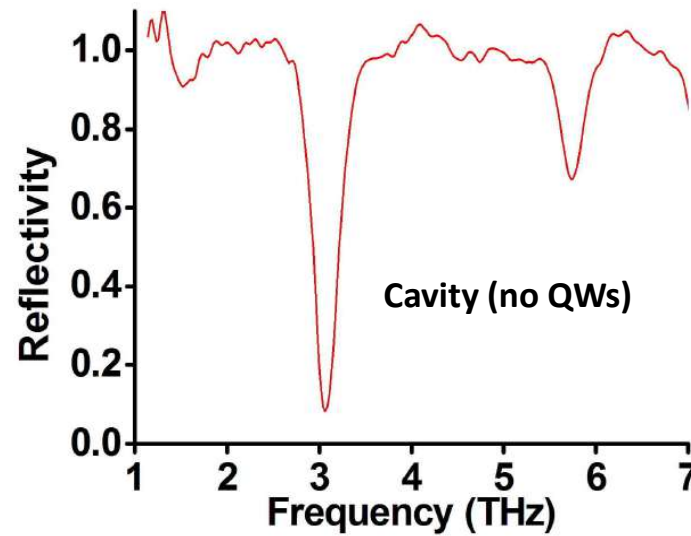
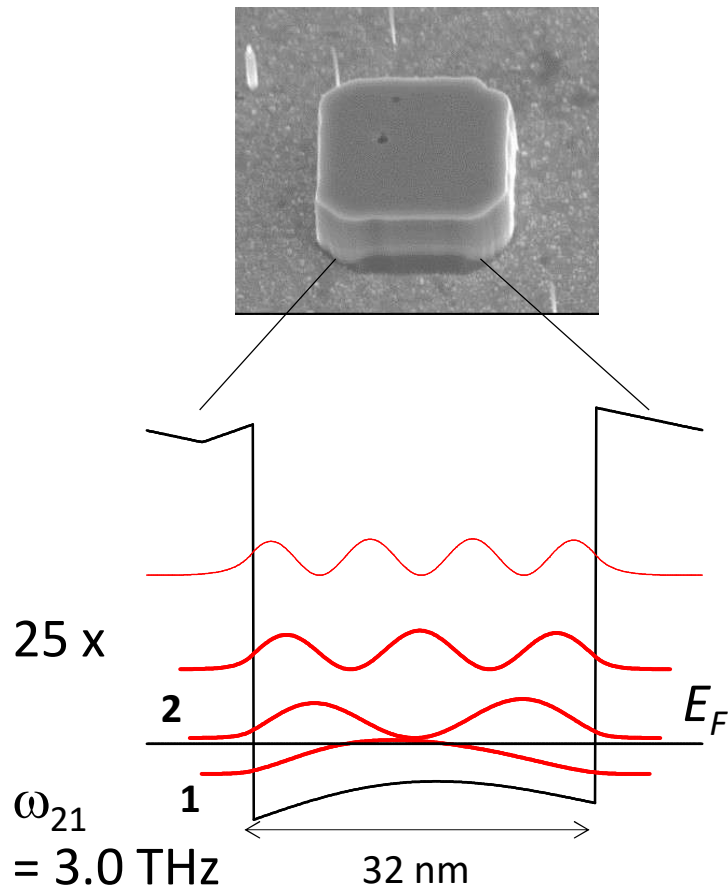
Modelling of:

- Absorption in cavity coupled devices (1)
- Saturation (2) and bistability (3,4)
- Non-linear generation (1)
- Advanced modelling of detectors (5)

1. T. Krieguer and Y. Todorov , Phys. Rev. B (2025)
2. M. Jeannin, et al. Phys. Rev. Lett. **127**, 187401 (2021)
3. M. Jeannin, et al. APL **122**, 241107 (2023)
4. Lin et al. APL Photonics **10**(4), (2025)
5. Pisani et al. Nature Comm. **14**, 3914 (2023)

Some applications

Ultra-strong light-matter coupling

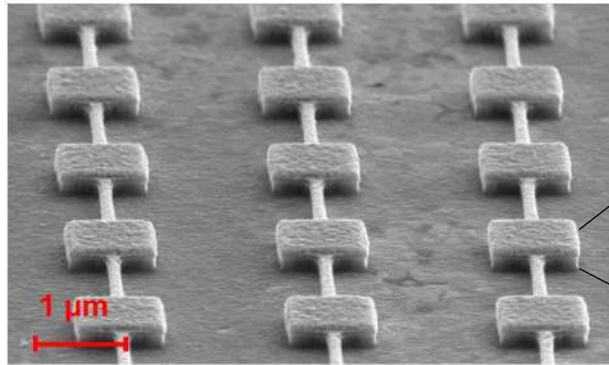
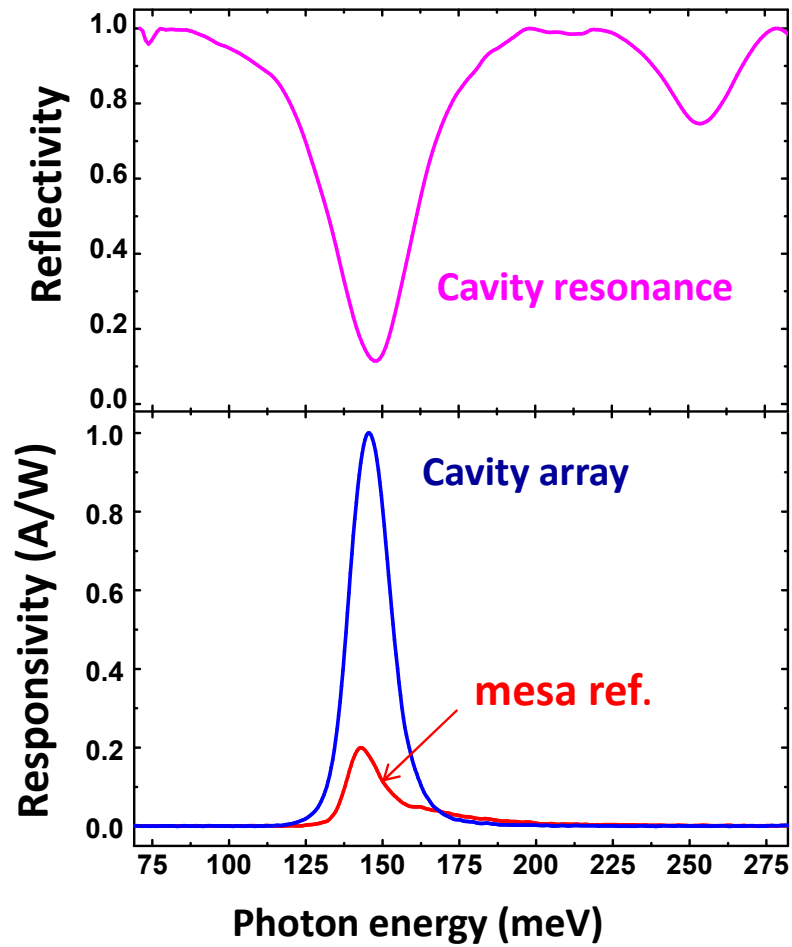


$$2\Omega_R / \omega_{21} = 0.46$$

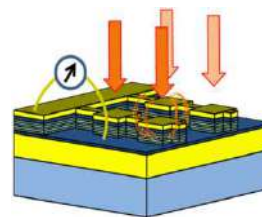
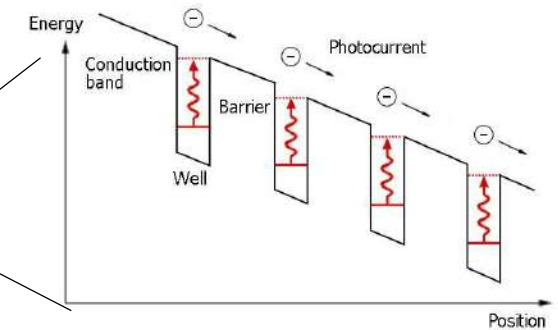
Todorov *et al.* PRL **102**,186402 (2009)

Todorov *et al.* PRL **105**,196402 (2010)

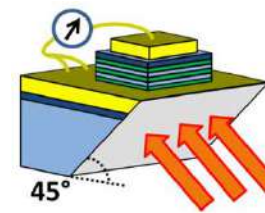
MIR detectors



QWIP detector



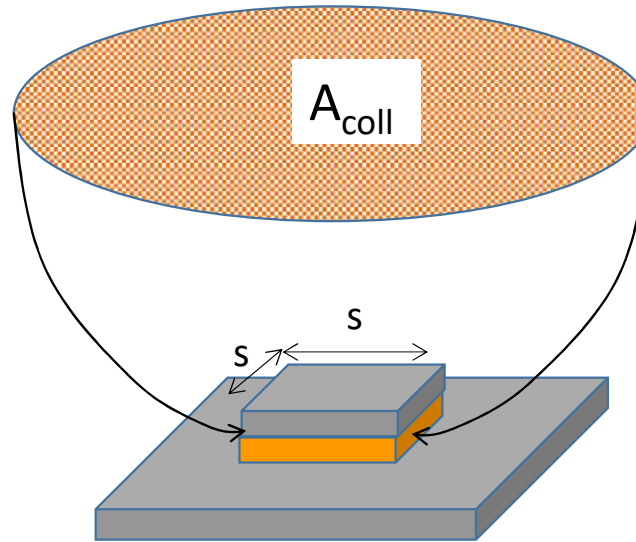
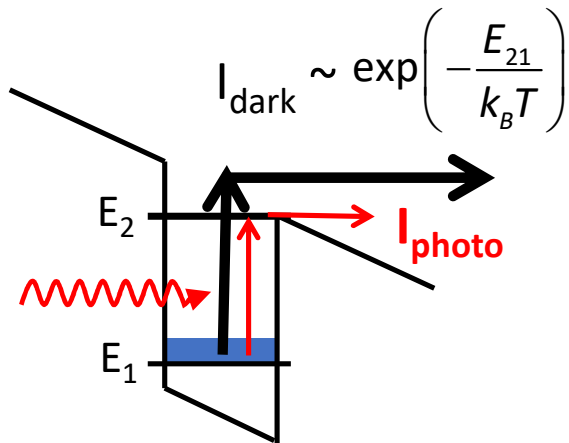
Cavity



mesa ref.

Y.-N. Chen *et al.* Appl. Phys. Lett. (2014)
D. Palaferri *et al.*, Nature (2018)

Dark current and Antenna effect



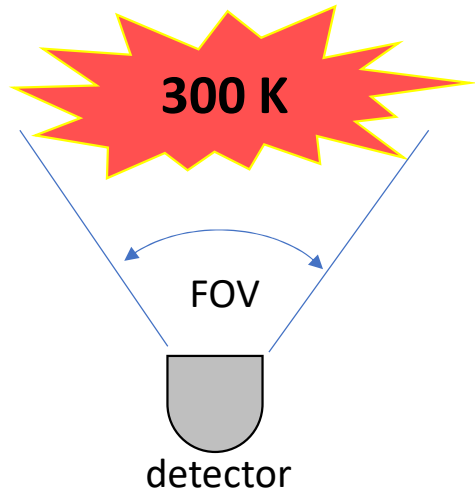
Can collect photons from an area larger than the metal pad!

$$I_{\text{photo}} \sim A_{\text{coll}} \times \text{photon flux}$$

$$I_{\text{dark}} \sim s^2 \exp(-E_{21}/k_B T)$$

-> Increased signal to noise ratio !

Impact on the temperature performance

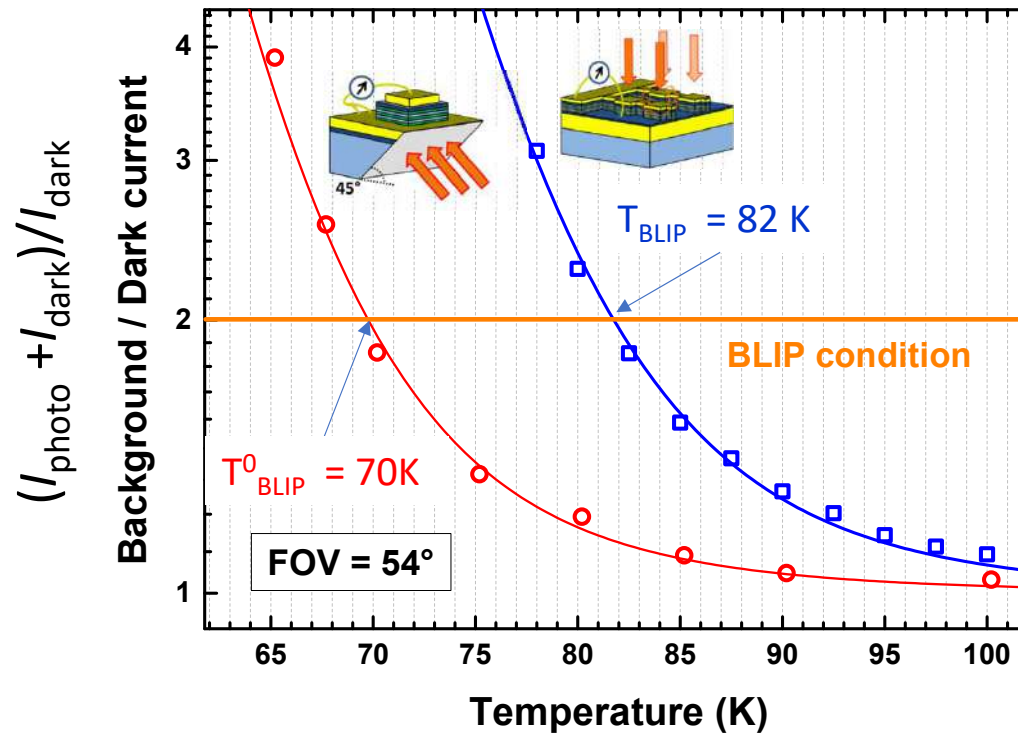


Responsivity
Ambient black body

$$I_{\text{photo}} = R\Phi_{300\text{K}}$$

$$I_{\text{dark}} \sim \exp(-E_{21}/k_B T)$$

$$I_{\text{photo}}(300\text{ K}) = I_{\text{dark}}(T_{\text{BLIP}})$$



Patch antenna detector:

$$T_{\text{BLIP}} \approx \frac{T_{\text{BLIP}}^0}{1 - \frac{k_B T_{\text{BLIP}}^0}{E_{21}} (\ln F - 1.8)}$$

$$F = \frac{\pi \epsilon |E_{\text{cav}}|^2}{|E_{\text{in}}|^2} = \frac{A_{\text{coll}} \lambda_{\text{res}}}{V_{\text{cav}}} Q$$

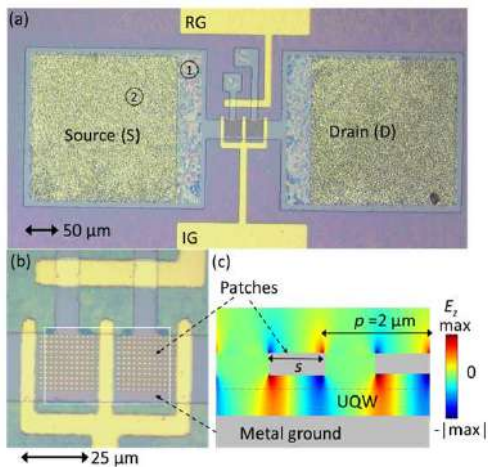
Local field enhancement

$$F \sim 350$$

Some further developments on patch-antenna coupled devices

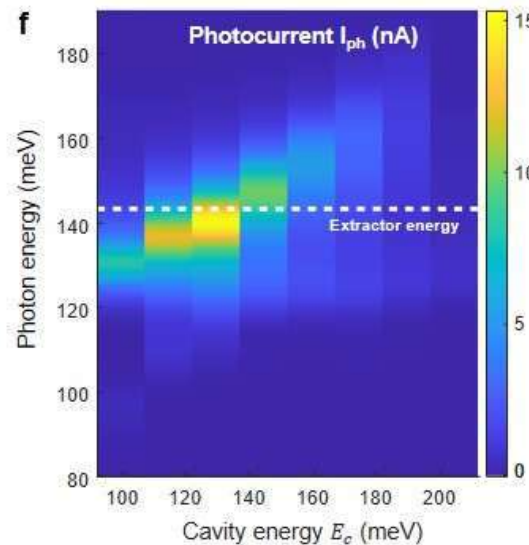
- Enhanced charge sensitive infrared phototransistors

Bahrehmand et al.
Appl. Phys. Lett. **127**, 011103 (2025)



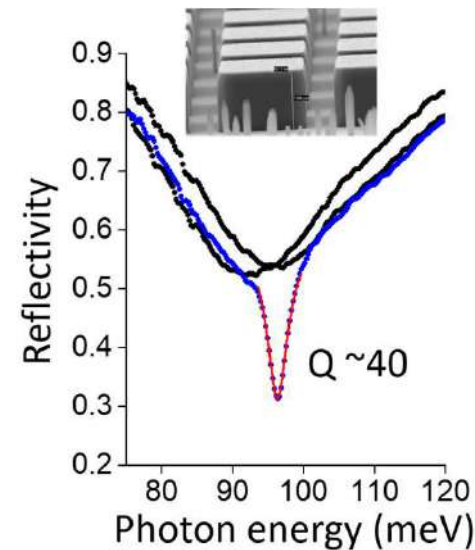
- SC with detectors

Francesco Pisani
(Nat. Comm, 2023)



- BIC in double-metal cavities

Pisani et al.
<https://arxiv.org/html/2607.13288v1>



ANR PRCI Gerald
Moustapha el Kurdi
PR Telecom Paris

Cavity-enhanced GeSn
devices

Other groups (non-exhaustive):

 S. Barbieri
High speed and
nonlinear detectors
Appl. Phys. Lett. 120, 091108 (2022)

 R. Colombelli
Polaritonic modulators
Appl. Phys. Lett. 125, 041101 (2024)

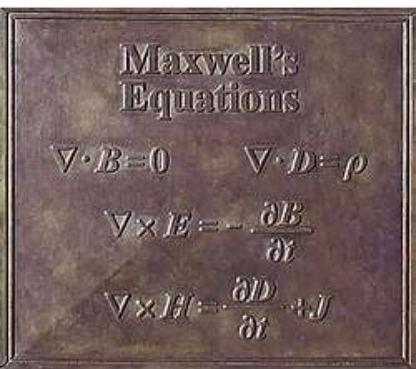
 B. Fix and
P. Bouchon
Multispectral IR absorbers,
NL generation, ...

 Y. Laplace

Plasmonic Cavities
Nature **656**, 343–348 (2026)

Summary

1. Introduction
2. Patch antenna cavities and their applications
3. THz “meta-atoms”



Optics and Electronics

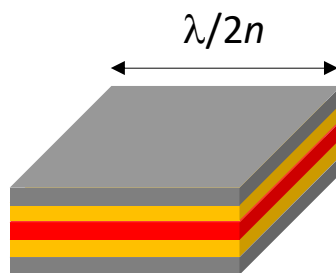
$$\nabla \times \mathbf{H} = \frac{\partial \mathbf{D}}{\partial t} + \mathbf{j}$$

displacement current

real current

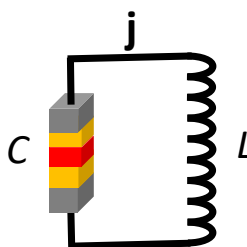
Patch Antenna

Inductor-capacitor circuit



Optics

$$\sigma \sim (\lambda/2n)^2$$



Electronics

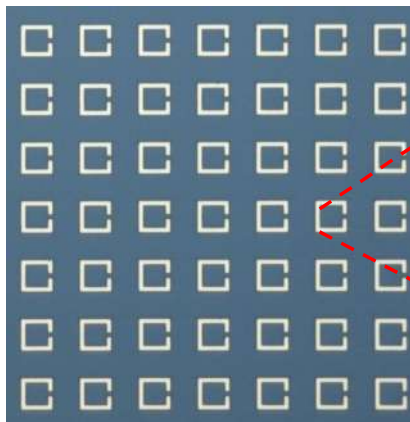
$$\sigma \ll (\lambda/2n)^2$$

Question:

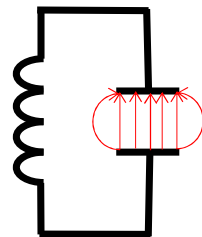
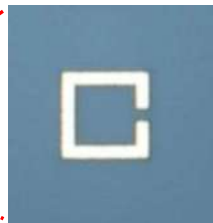
How can we
Implement
A THz LC circuit?

Metamaterials and meta-atoms:

Metamaterials



“meta-atom”



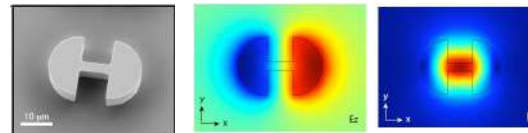
**strong electric
field in the capacitor**

W. Cai and V. M. Shalae, *Optical Metamaterials: Fundamentals and Applications* (Springer, 2009).

J.B. Pendry, A.J. Holden, D.J. Robbins, and W.J. Stewart, *IEEE Trans. Microwave Theory Tech.* **47**, 2075 (1999).

Implementations in the THz & MIR:

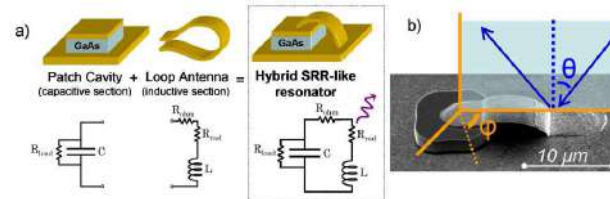
- LC-like patch cavities



C. Walther *et al.* *Science* (2010)

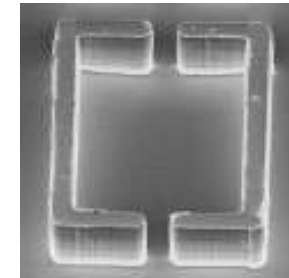
J. Faist's group (ETH Zurich)

- « Inverted » meta-materials



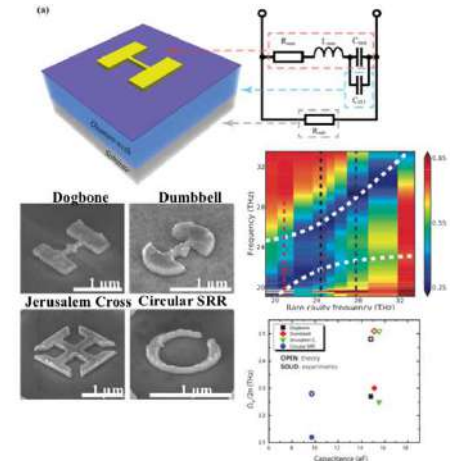
B. Paulillo *et al.* *Opt. Express*, **22**, 21302 (2014)

B. Paulillo *et al.* (2016) “Terahertz meta-atom quantum well photodetectors” *Lasers and Electro-Optics (CLEO)*, USA 2016



D. Dietze, *et al.*

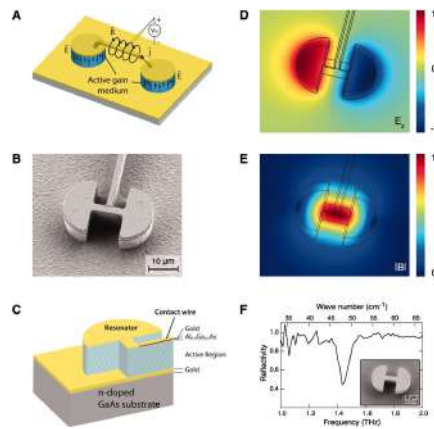
Appl. Phys. Lett. 103, 201106 (2013)



Igal Brener's group, Sandia Labs

Some THz (LC) meta-atoms:

Quantum cascade lasers



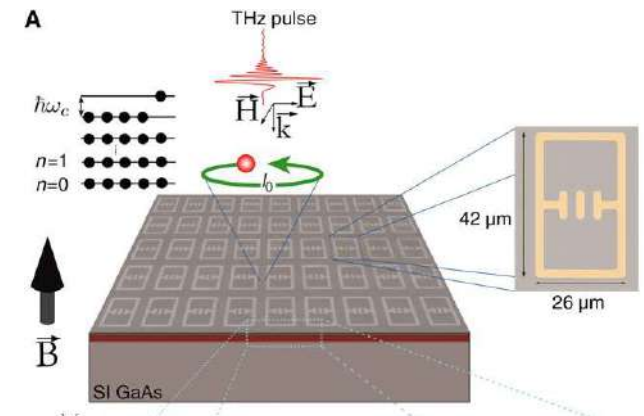
C. Walther *et al.*
Science (2010)

THz detectors



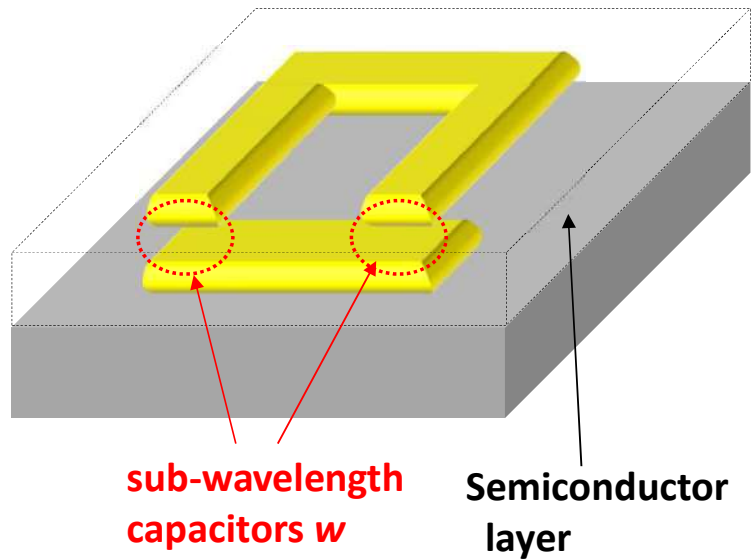
Jeannin *et al.*,
Appl. Phys. Lett. **117**, 251102 (2020)

Ultra-strong light-matter coupling



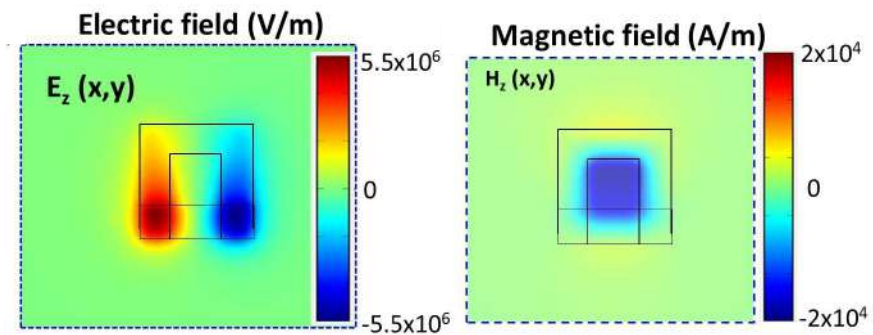
Scalari *et al.*
Science (2012)

The idea



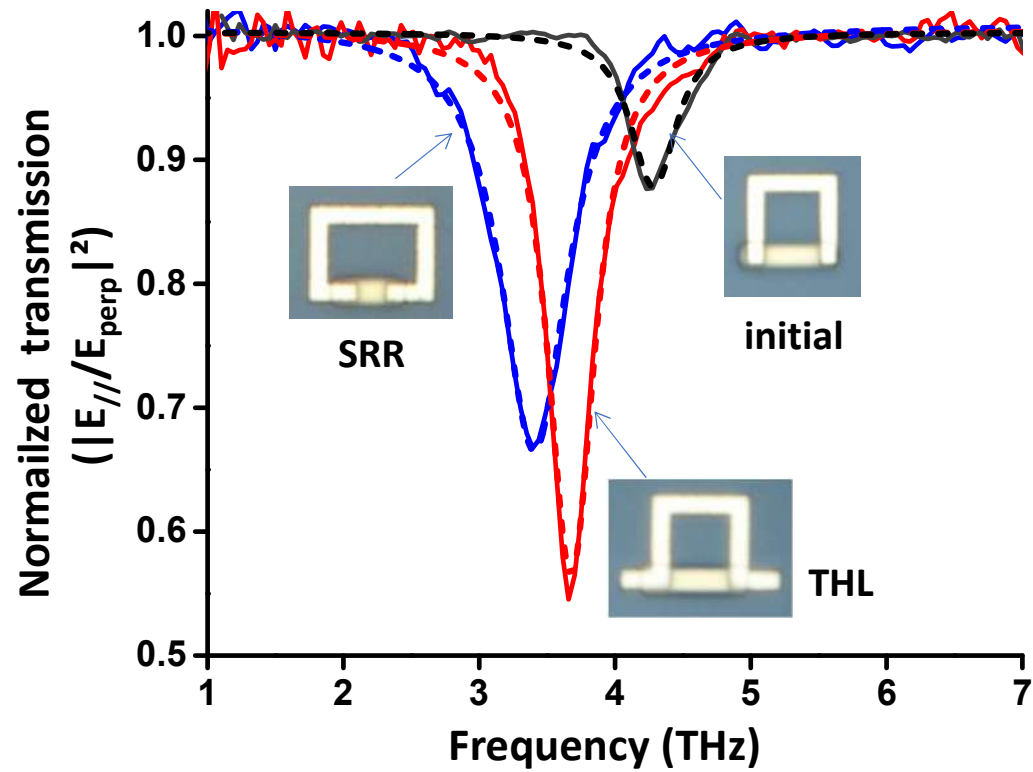
Advantages:

- Highly sub-wavelength confinement
- Propagation effects minimized
- **Easy implementation of DC electrical pump/read-out**

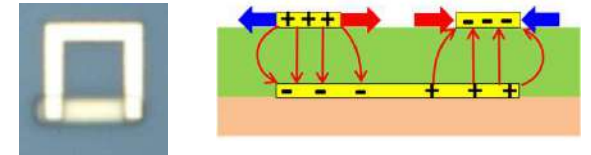


Y. Todorov, *Opt. Express*. **23**, 16839-16845 (2015)
A. Mottaghizadeh, *Opt. Express*. **25**, 28718-28730 (2017)
O. Mitrofanov, *Opt. Express*. **26** 7437-7450 (2018)

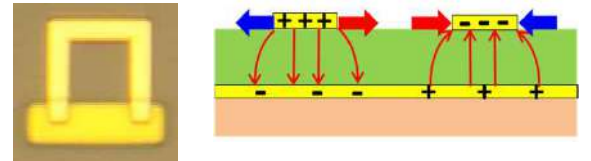
Geometrical explorations



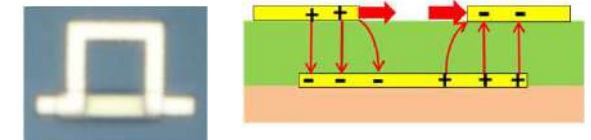
Initial design



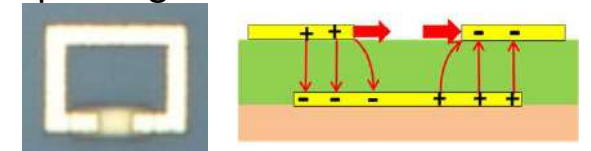
Dark mode



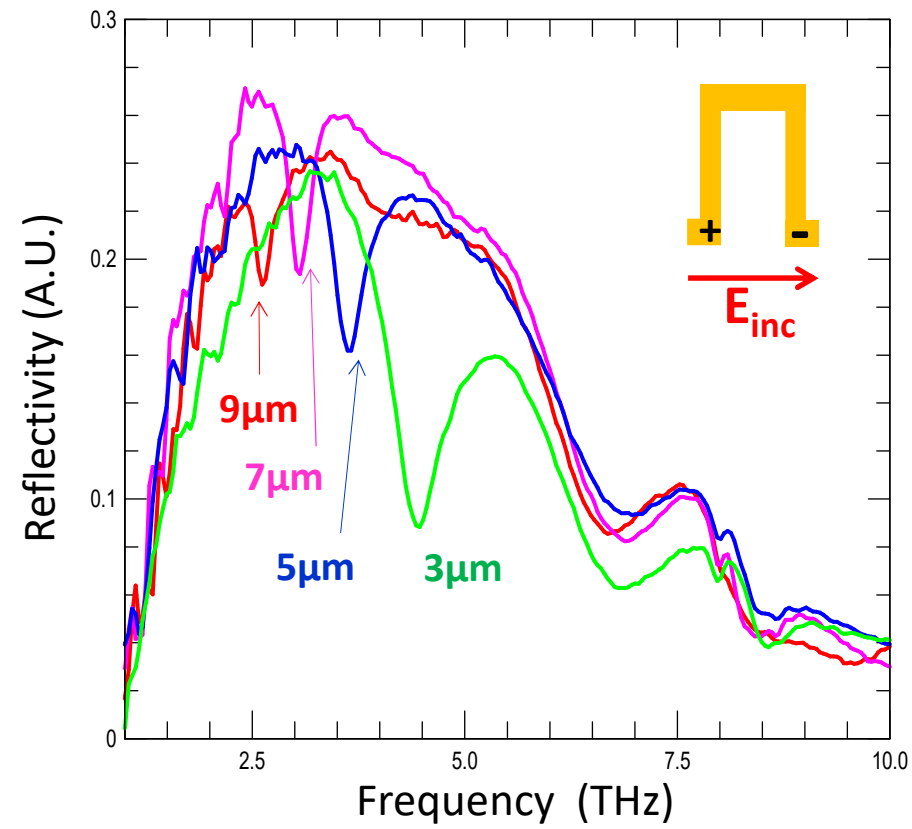
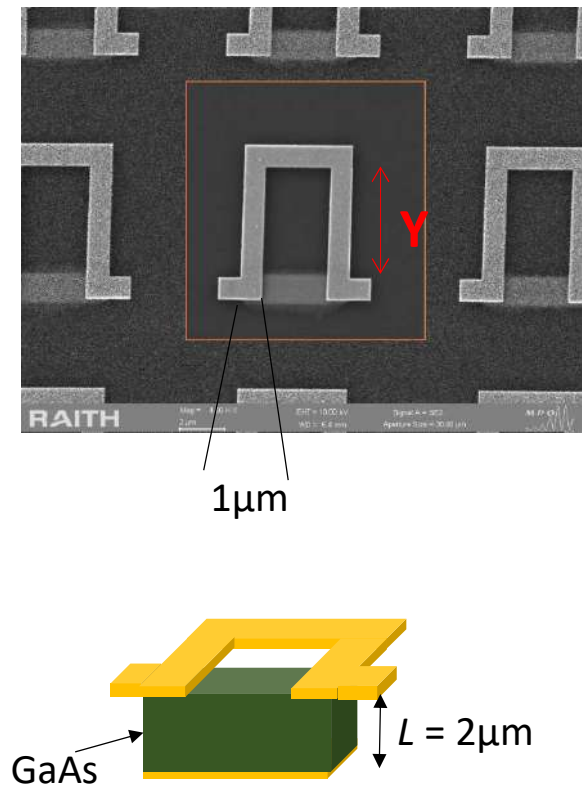
Top hat loop



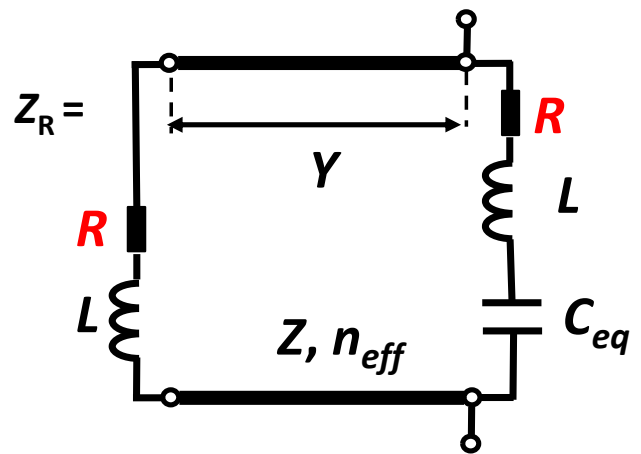
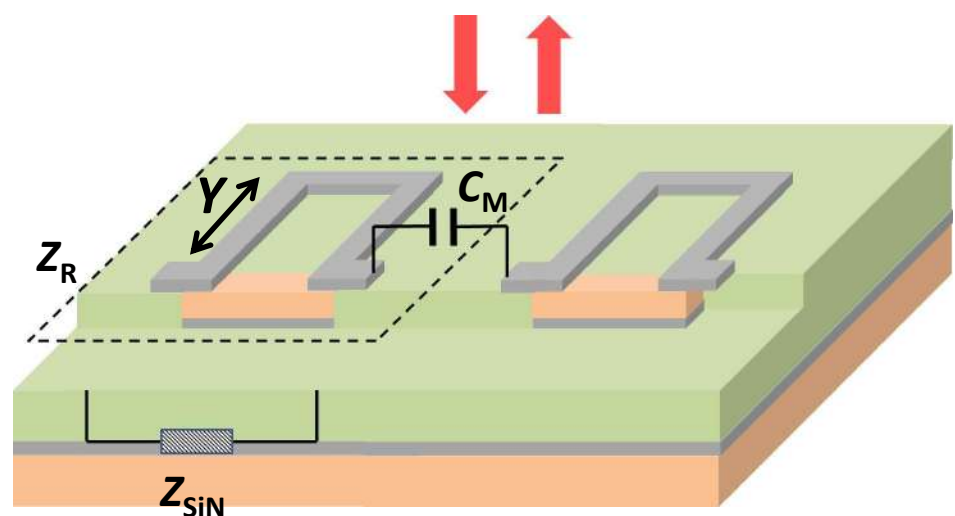
Split ring



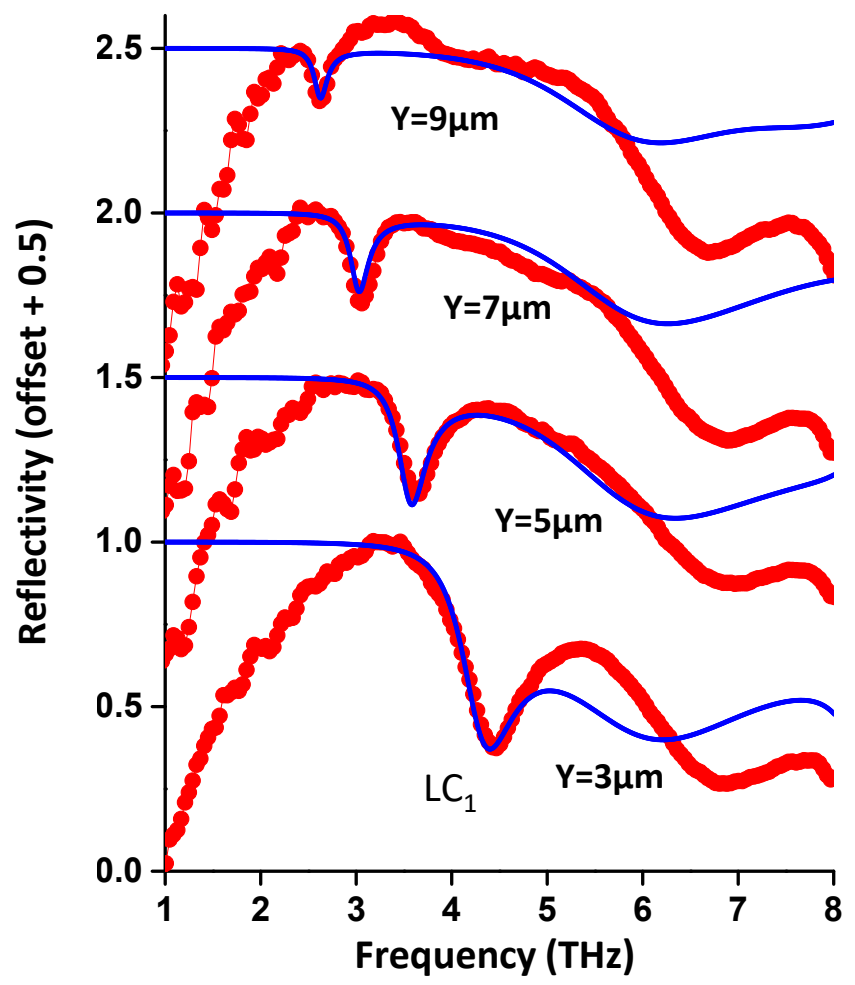
Resonance tuning



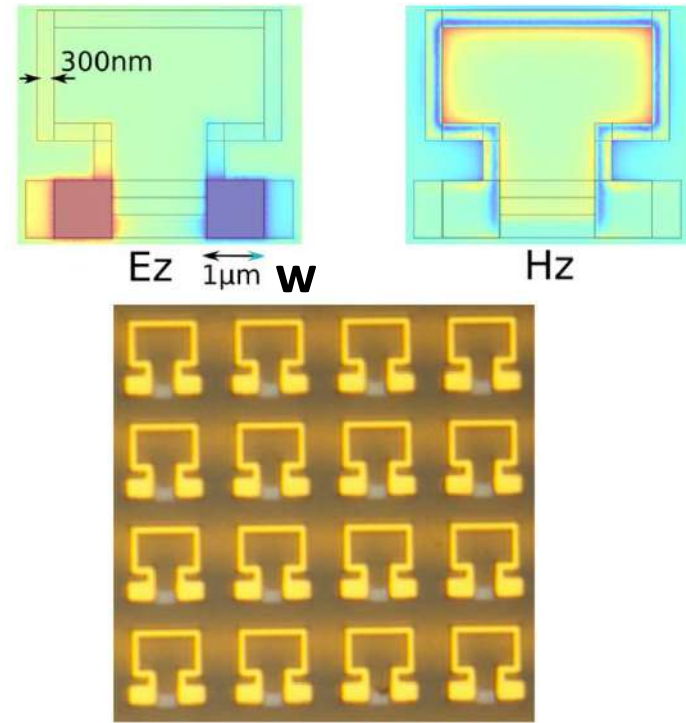
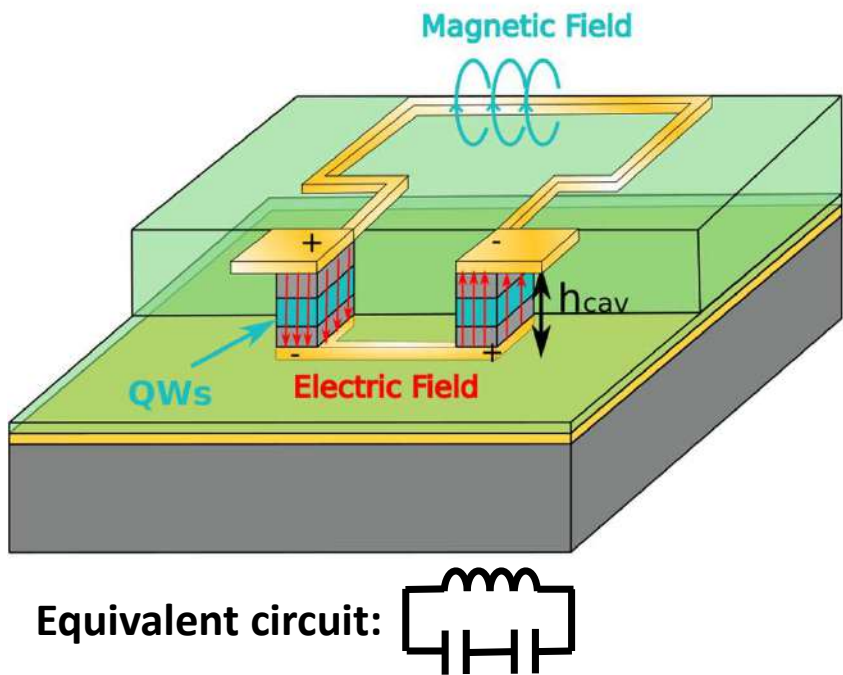
Equivalent circuit model



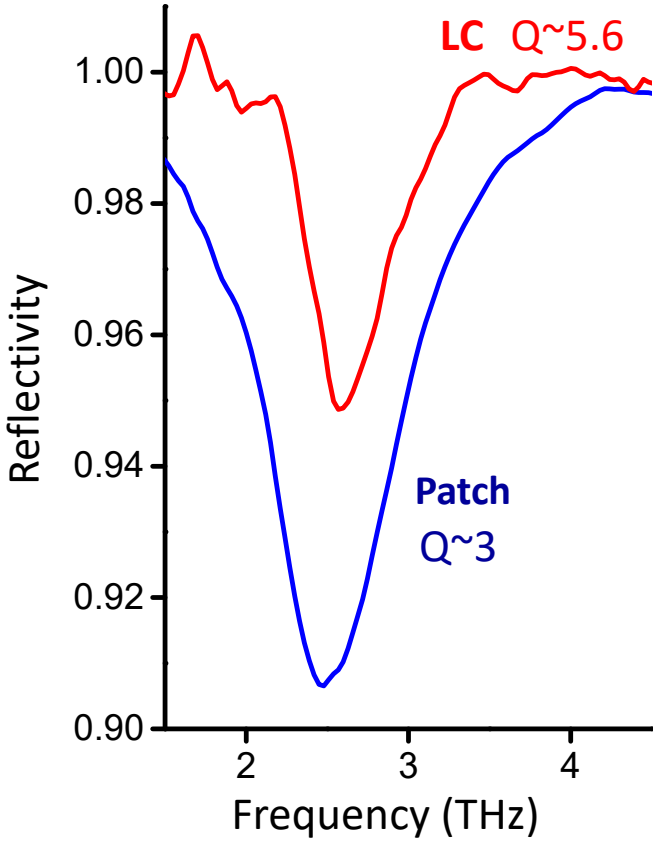
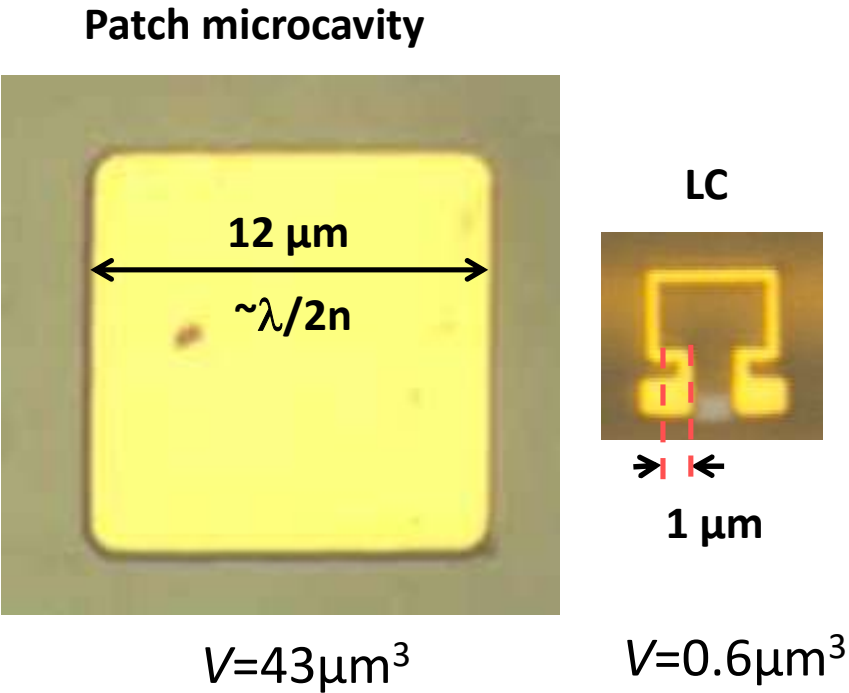
Resonator non-radiative loss dominated by the resistance of the inductive elements!



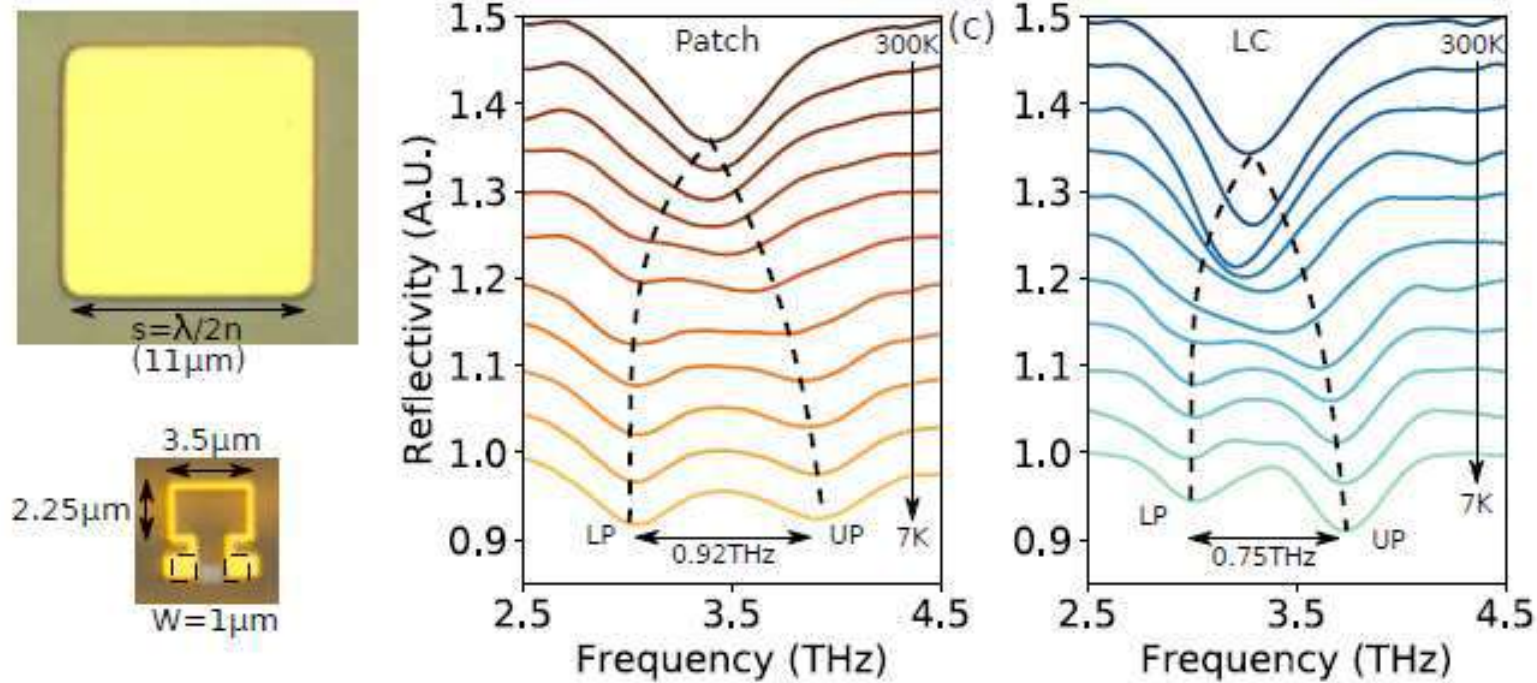
An optimized THz LC meta-atom



Comparison with patch-antennas

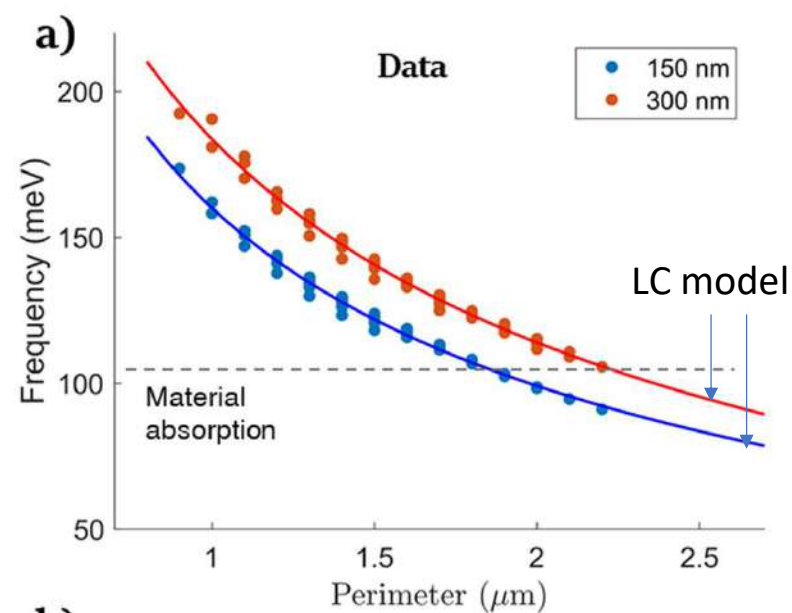
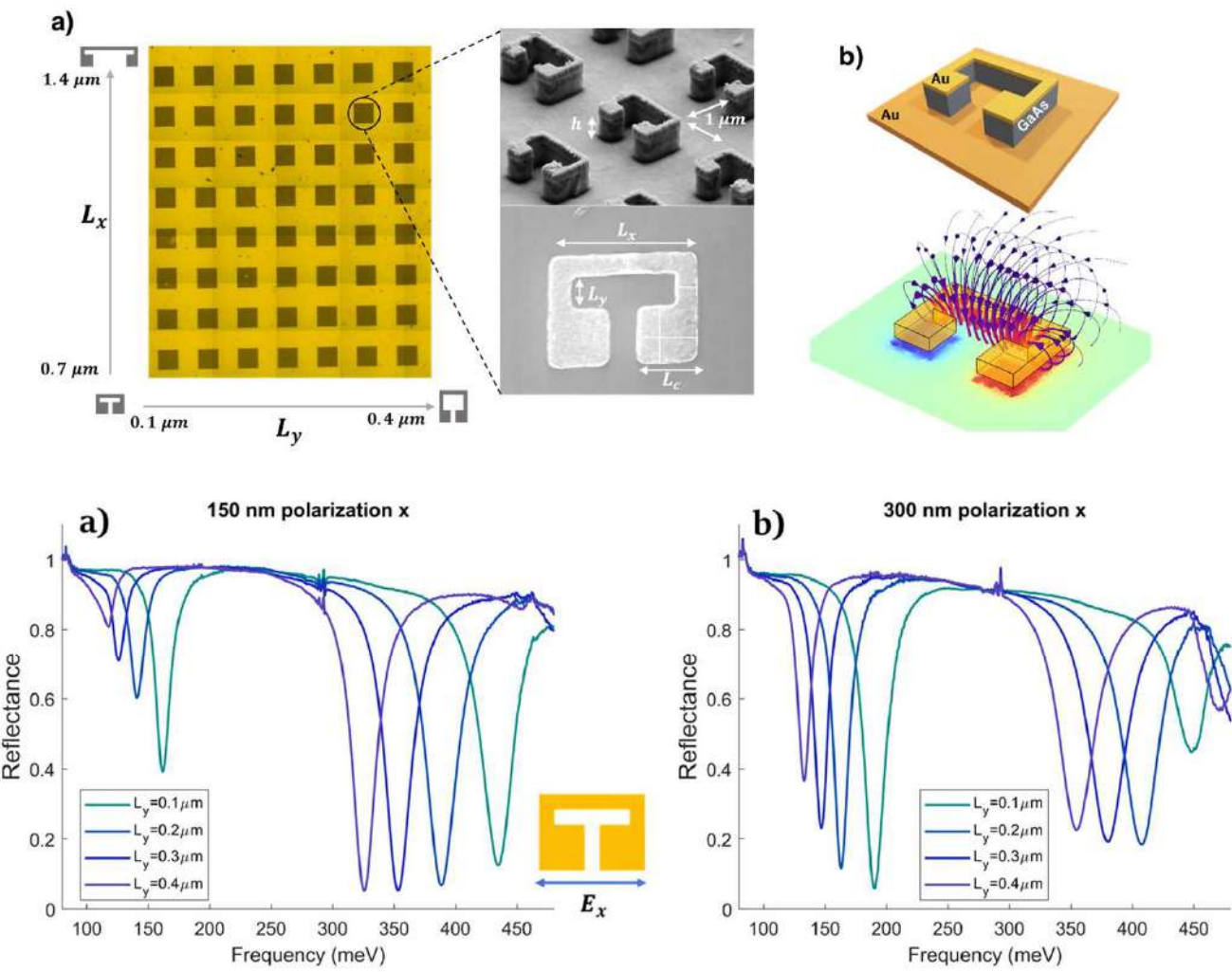


Polariton splitting: attesting the subwavelength confinement



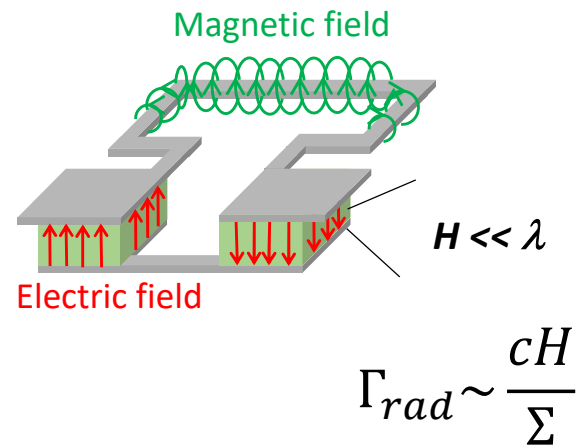
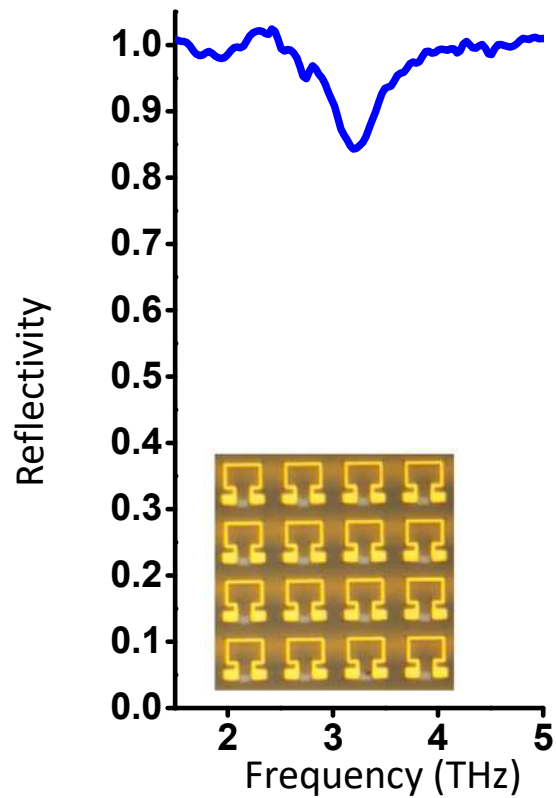
$$\hbar\Omega_{\text{Rabi}} \propto \sqrt{\frac{N_{\text{electrons}}}{V_{\text{cavity}}}} = \text{const} \quad , \text{ but } V \text{ is much smaller!}$$

Works also for the MIR range (10x shorter wavelengths)

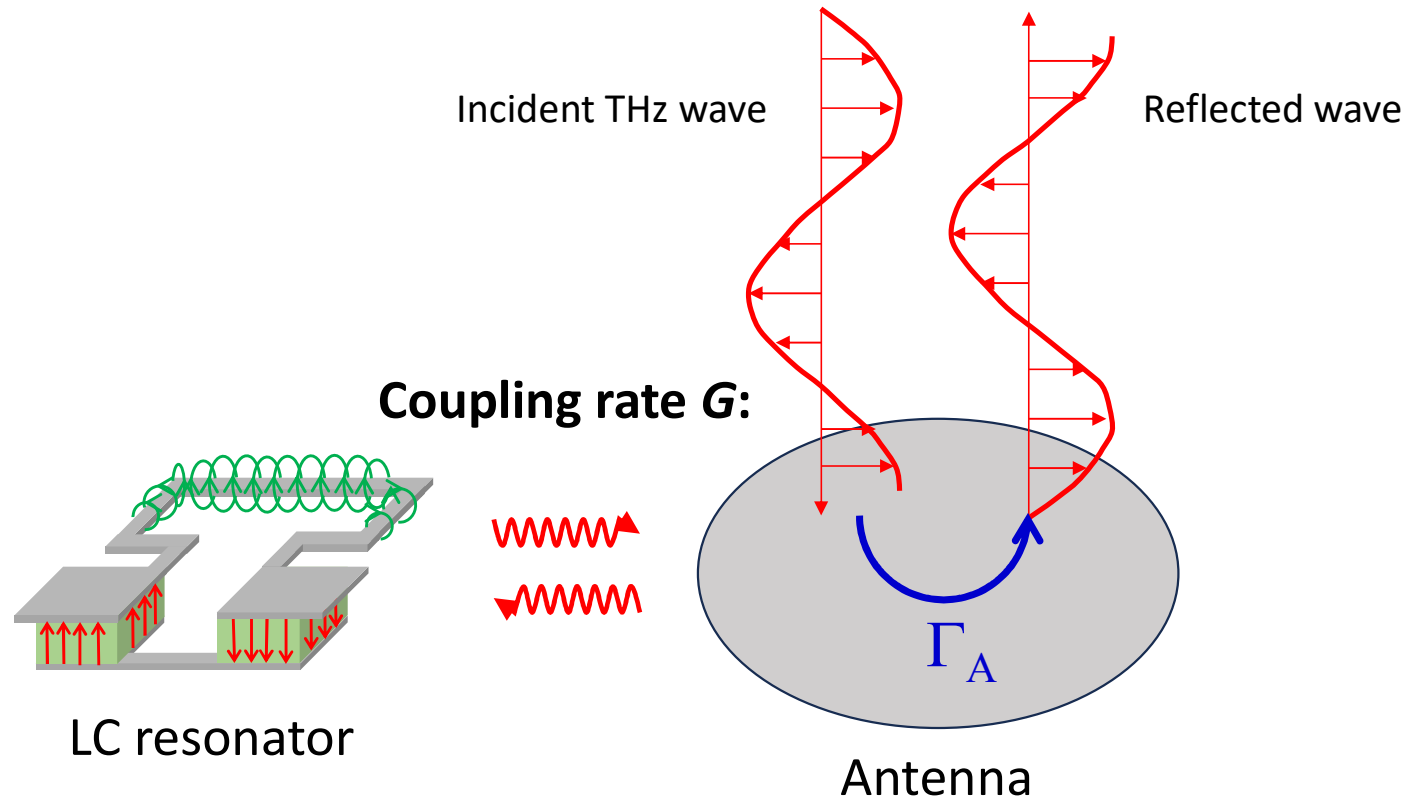


3D Meta-Atoms for High Confinement of Mid-IR Radiation
F. Pisani, et al. ADOM (2025)

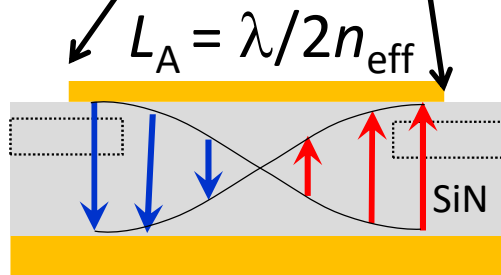
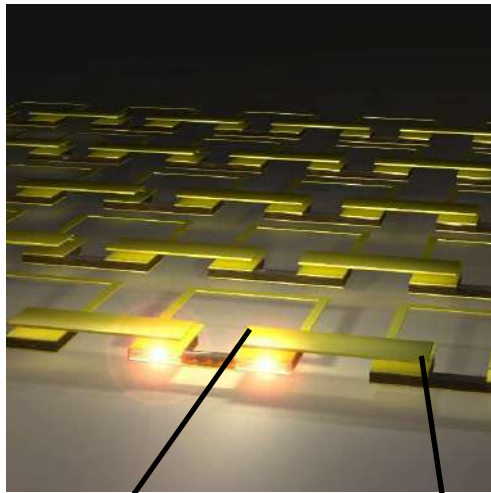
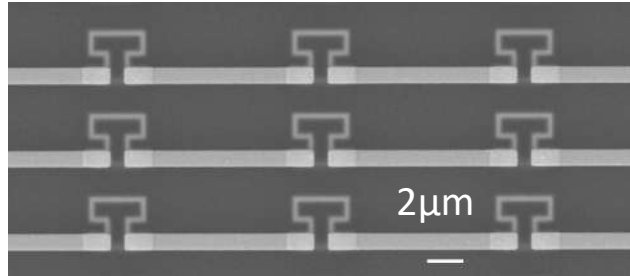
Problem: very low radiation loss...



Idea: couple the resonator with an element that has high radiation loss

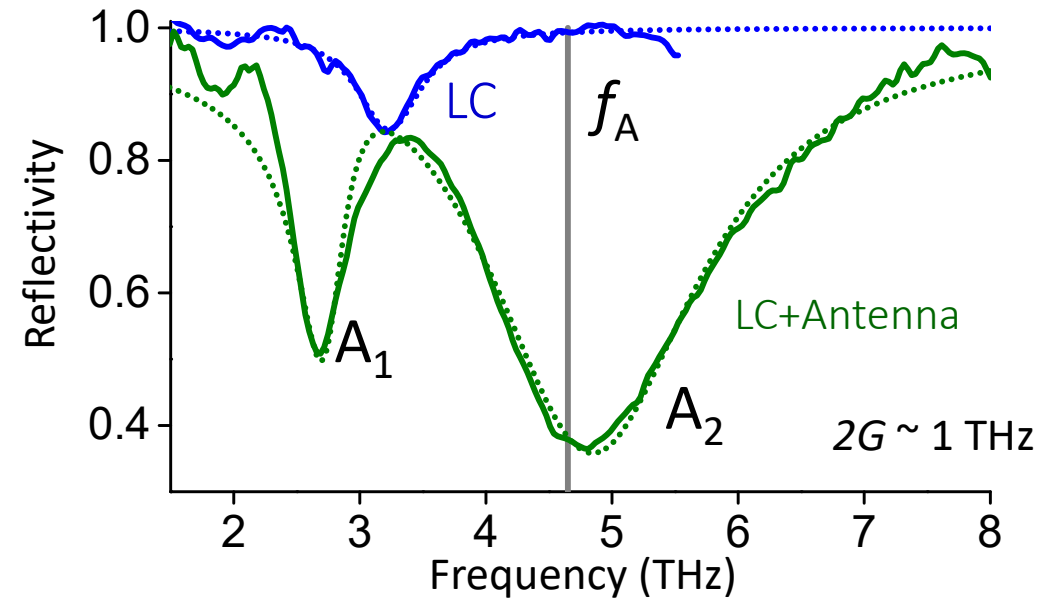


Side-coupling to wire patch antennas

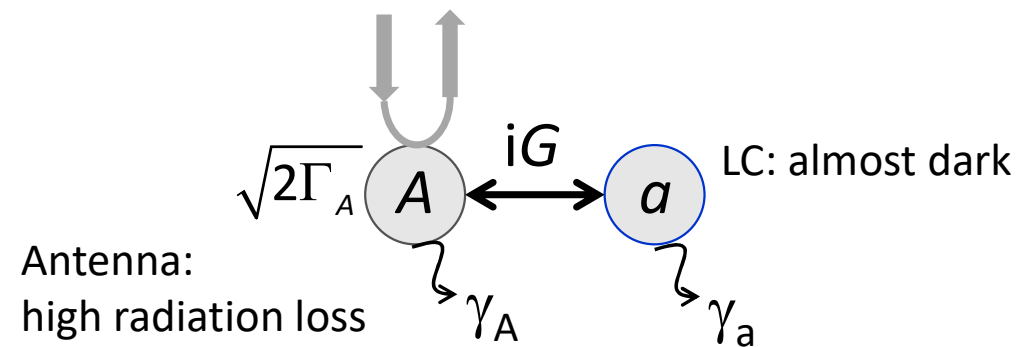


"Wire" patch antenna

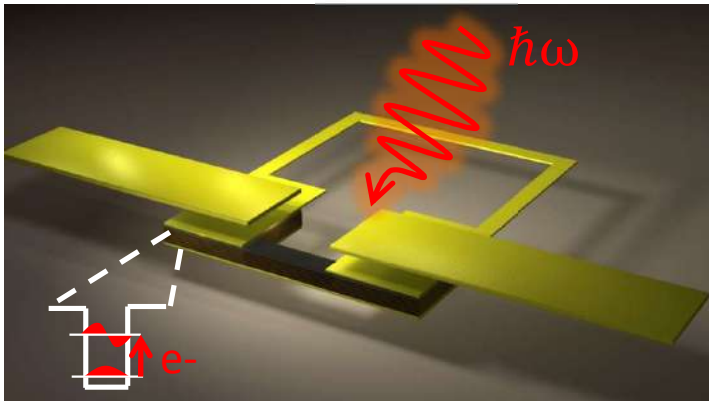
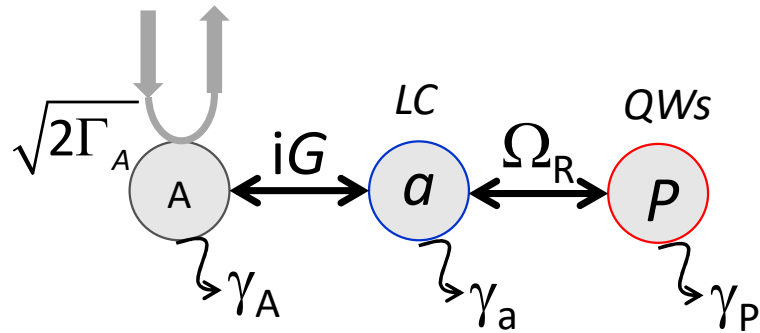
M. Jeannin et al. Nano Lett. **20**(6), 4430–4436 (2020)



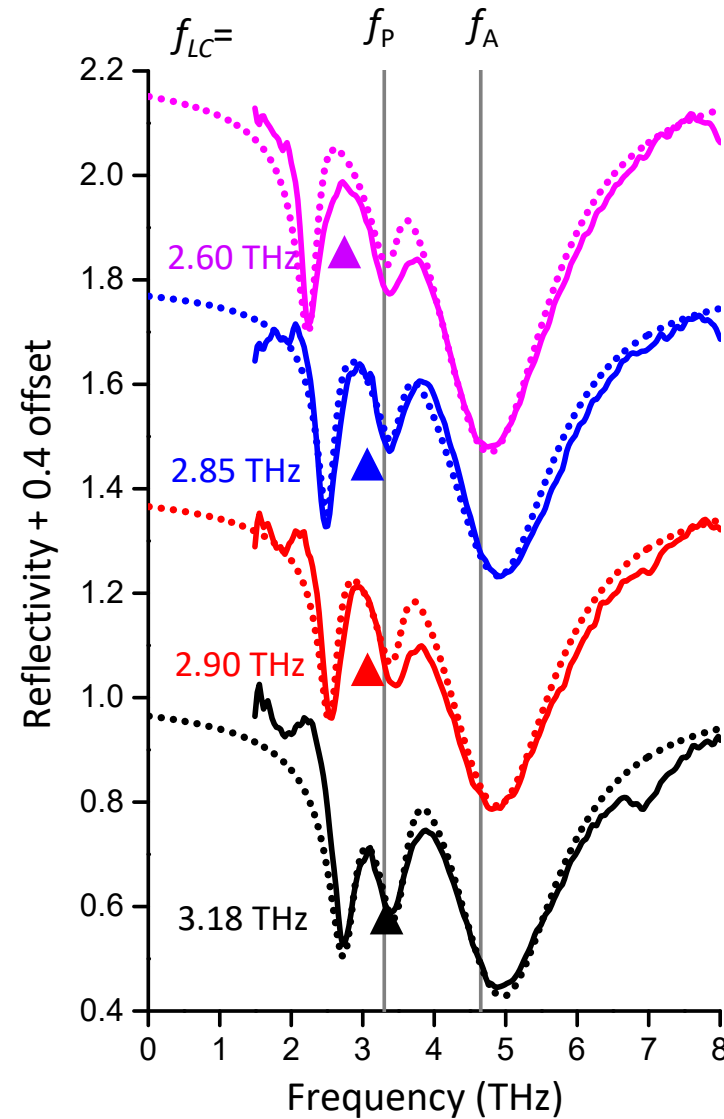
Coupled-Mode theory diagram:



Strong coupling with QW: the mode volume is preserved



M. Jeannin et al. Nano Lett. **20**(6), 4430–4436 (2020)

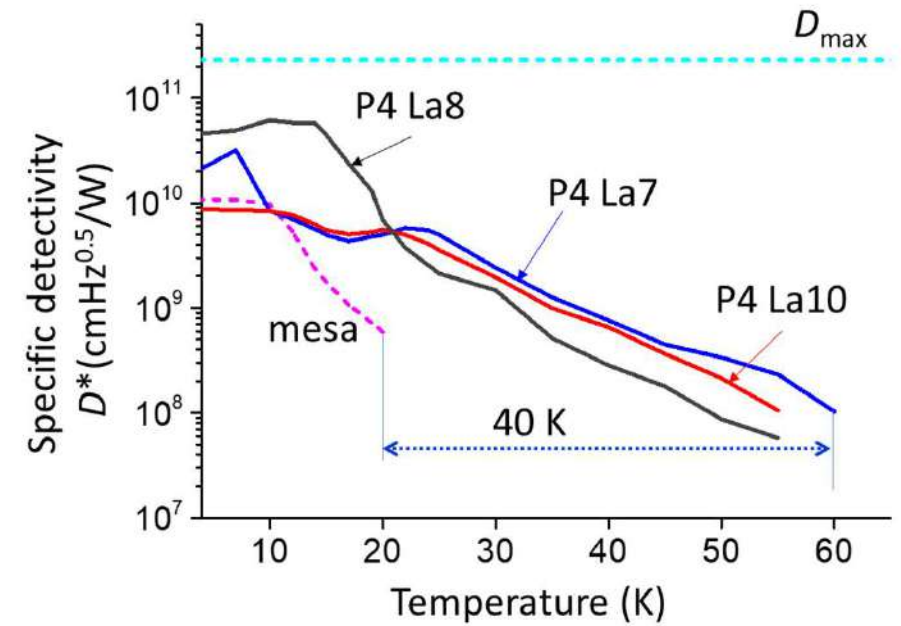
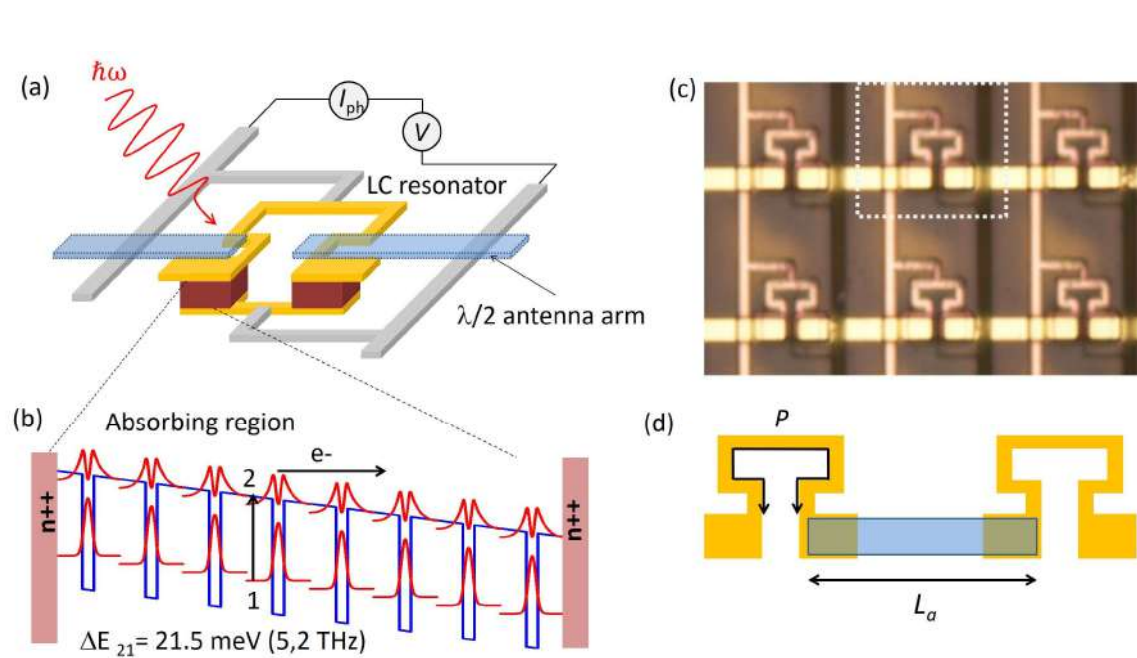


The same Ω_R is obtained as in the case without antenna:

Sub-wavelength confinement is preserved!

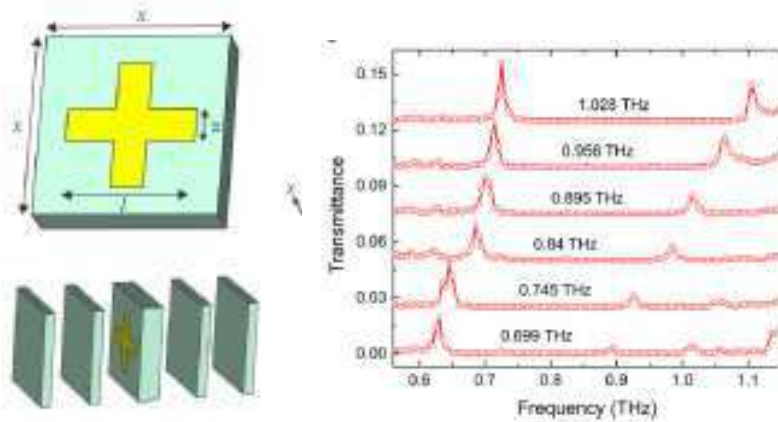


Application for THz detection



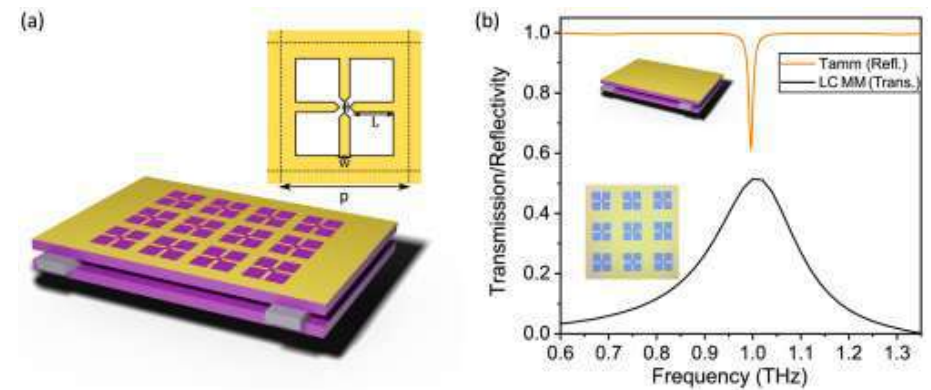
Recent developments on coupled THz resonators

- Coupling between SRRs and Bragg Cavities
Hartmut Roskos, Goethe-University Frankfurt am Main



F. Meng, et al. ,” Opt. Express 29, 42420–42434 (2021)

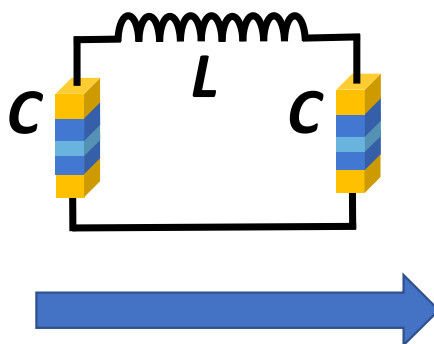
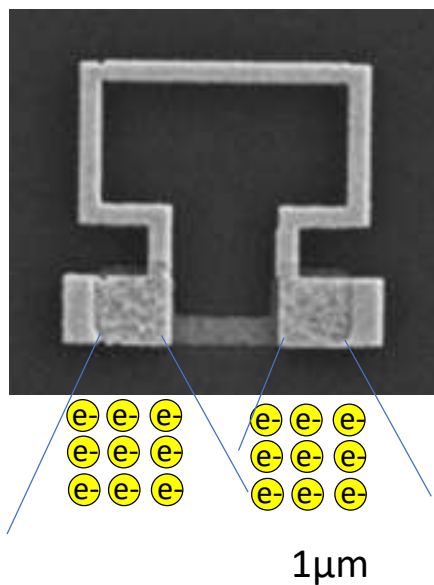
- Low mode volume and High-Q factors
Juliette Mangeney , LPENS (Paris)



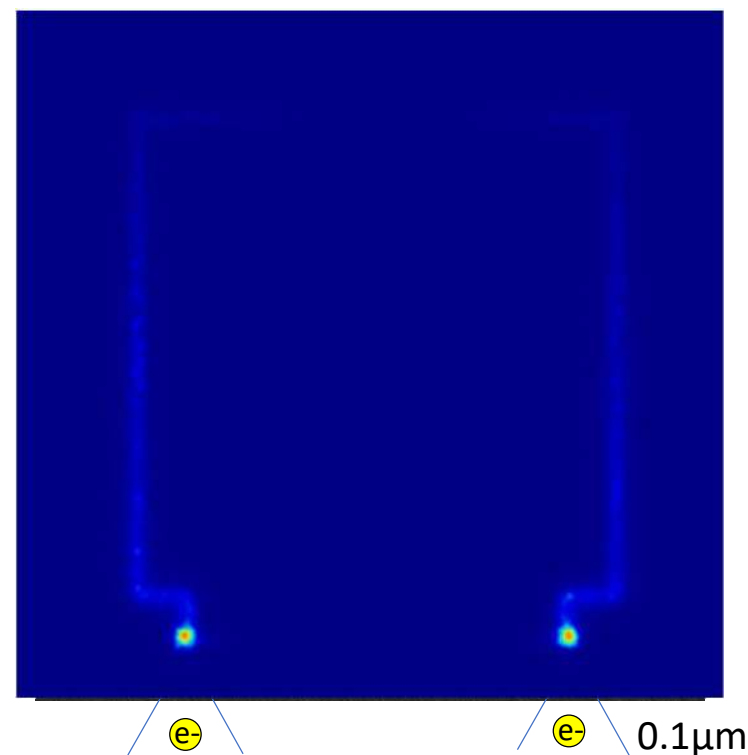
Messelot, et al. Photon. Res. 11, 1203-1216 (2023)

Towards quantum effects in THz metamaterials

Ultra-strong light-matter coupling with THz meta-atoms: **single electron limit?**

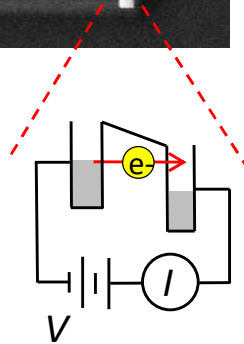
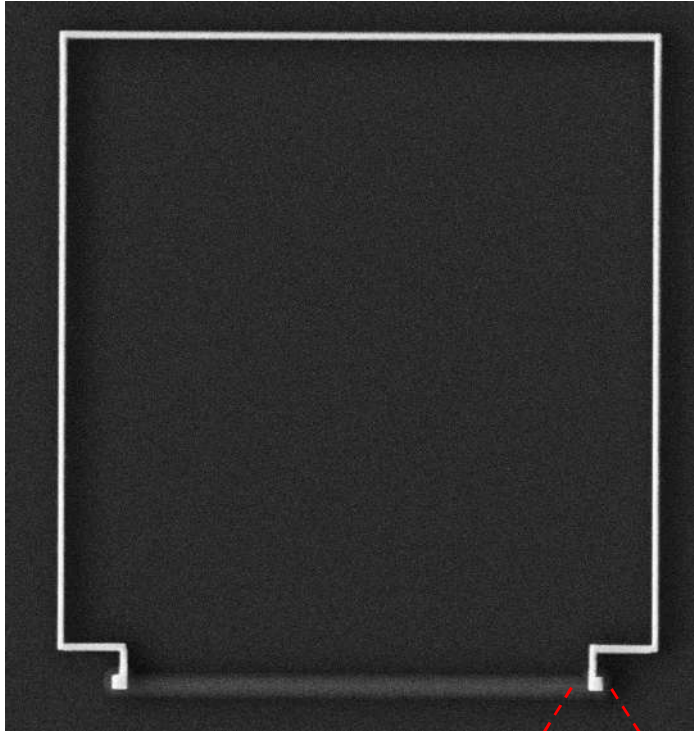


$$\omega_{LC} = \frac{1}{\sqrt{LC}}$$



$$\frac{\Omega_R^2}{\omega_{12}^2} \approx \frac{e^2/2C}{\hbar\omega_{LC}} = \rho_0$$

Single electron limit with a metamaterial coupled tunnel junction



$$\frac{\Omega_R^2}{\omega_{12}^2} \approx \frac{e^2/2C}{\hbar\omega_{LC}}$$

Electrostatic energy of a single electron

Oscillation quantum of the circuit

VOLUME 64, NUMBER 15

PHYSICAL REVIEW LETTERS

9 APRIL 1990

Effect of the Electromagnetic Environment on the Coulomb Blockade in Ultrasmall Tunnel Junctions

M. H. Devoret,⁽¹⁾ D. Esteve,⁽¹⁾ H. Grabert,⁽²⁾ G.-L. Ingold,⁽²⁾ H. Pothier,⁽¹⁾ and C. Urbina⁽¹⁾

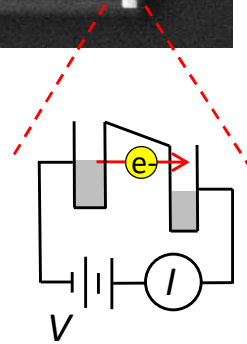
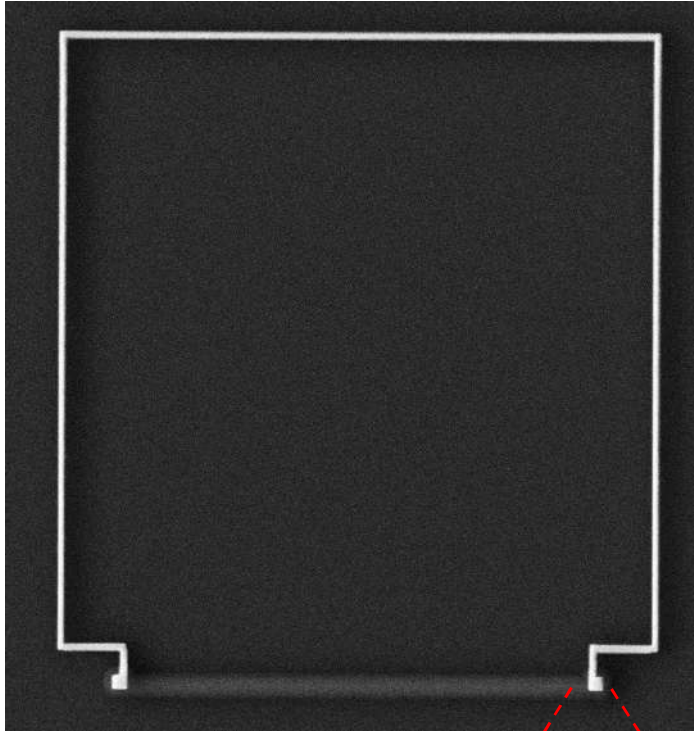
⁽¹⁾*Service de Physique du Solide et de Résonance Magnétique, Centre d'Études Nucléaires de Saclay, 91191 Gif-sur-Yvette, France*

⁽²⁾*Fachbereich Physik, Universität-Gesamthochschule Essen, 4300 Essen, Federal Republic of Germany*
(Received 4 December 1989)

Quantum Fluctuations of the LC resonator charge: $\Delta Q^2 = C \frac{\hbar\omega_{LC}}{2}$

If $\Delta Q < e$ the conductance is blocked!

Single electron limit with a metamaterial coupled tunnel junction



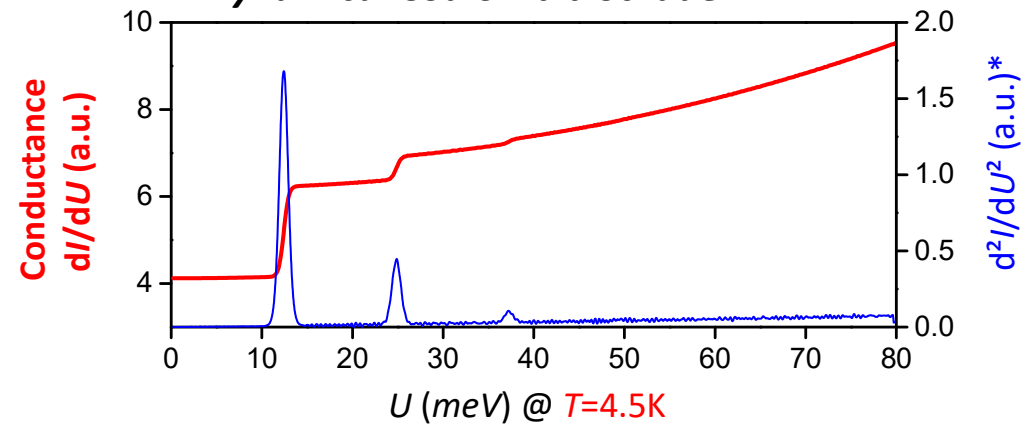
$$\frac{\Omega_R^2}{\omega_{12}^2} \approx \frac{e^2/2C}{\hbar\omega_{LC}}$$

Electrostatic energy of a single electron

Oscillation quantum of the circuit

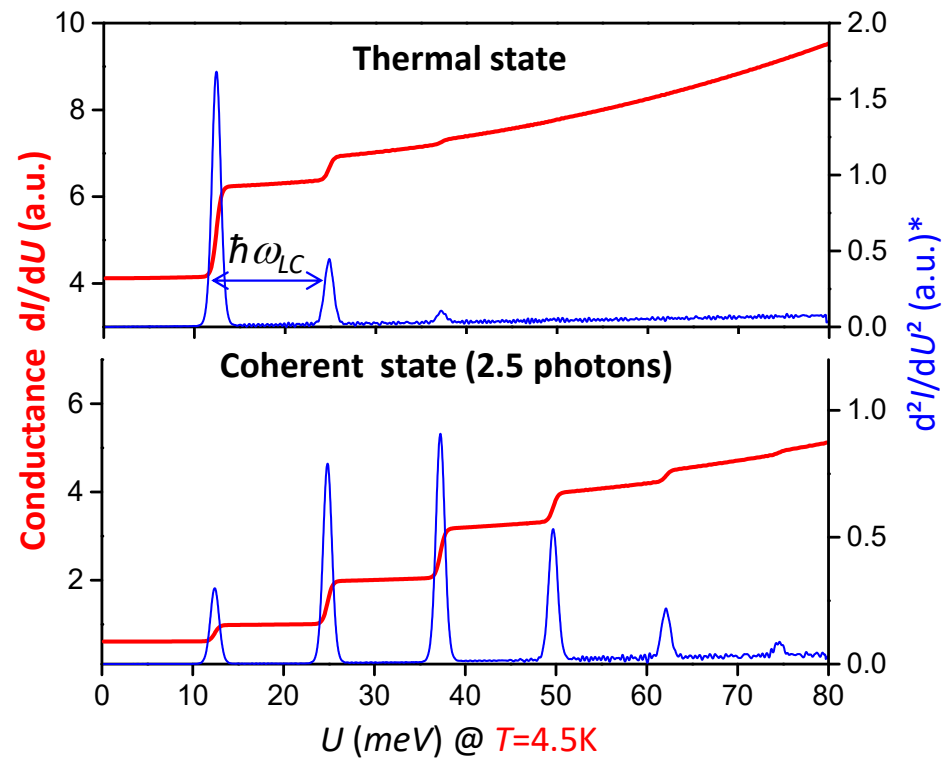
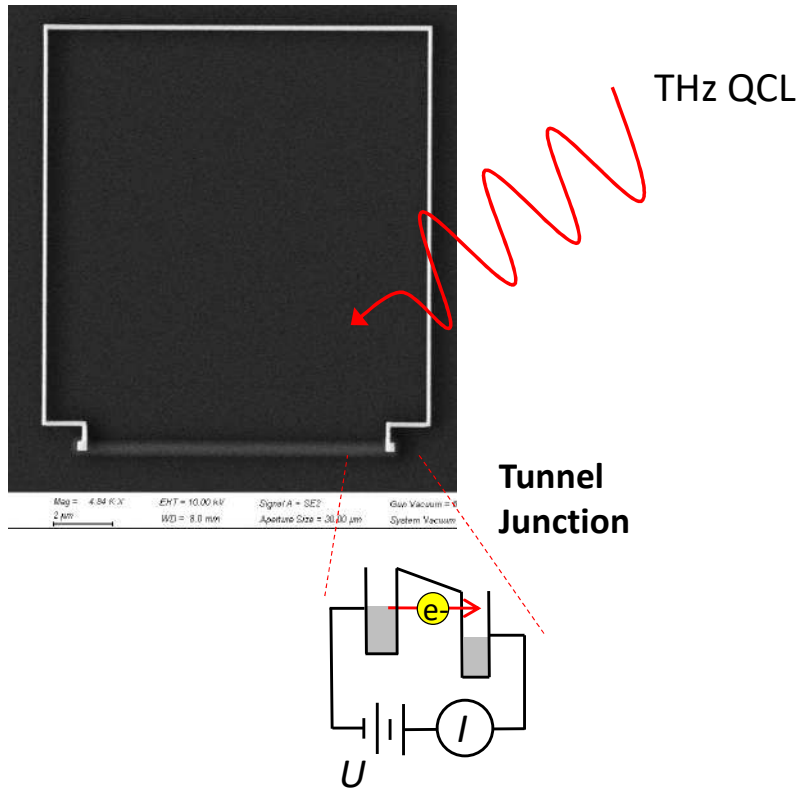
The DC conductance is sensitive to the vacuum fluctuations of the circuit

Dynamical Coulomb blockade



Single electron limit with a metamaterial coupled tunnel junction

Read-out of the quantum state of incident THz photons



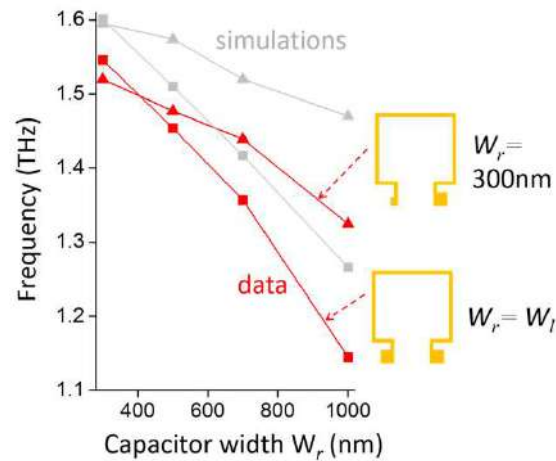
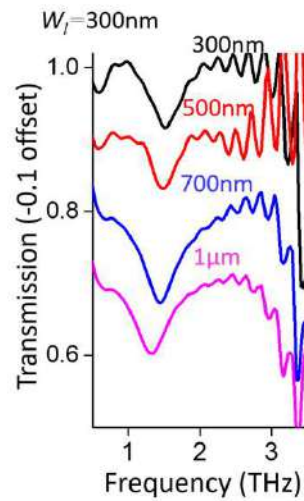
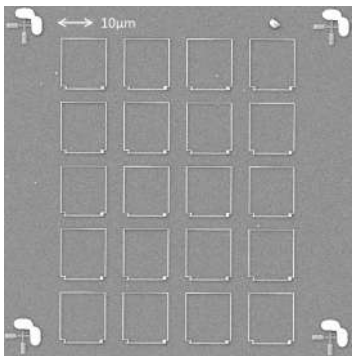
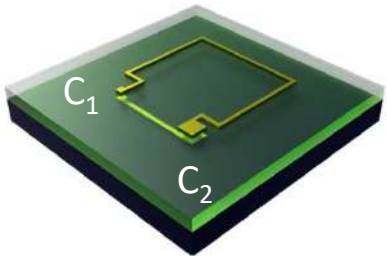
J.-R. Souquet et al., Nat. Comm. **5**, 5562 (2014)

U. Iqbal, C. Mora, and Y. Todorov, Phys. Rev. Research **6**, 033097 (2024)

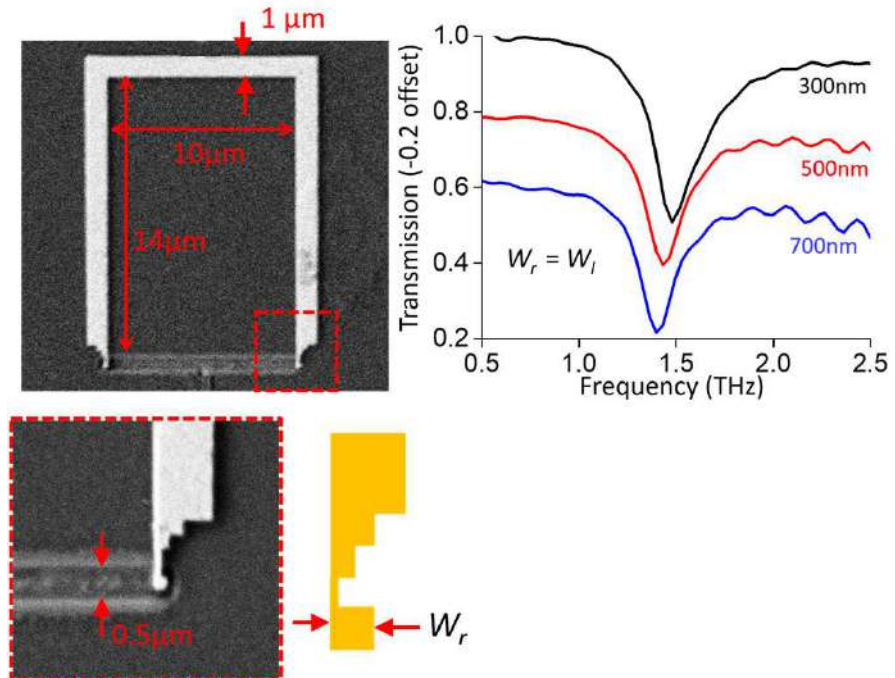
THz meta-atoms in nanoscale capacitors

Iqbal et al., Optics Express **34**, pp. 30442-30454 (2026)

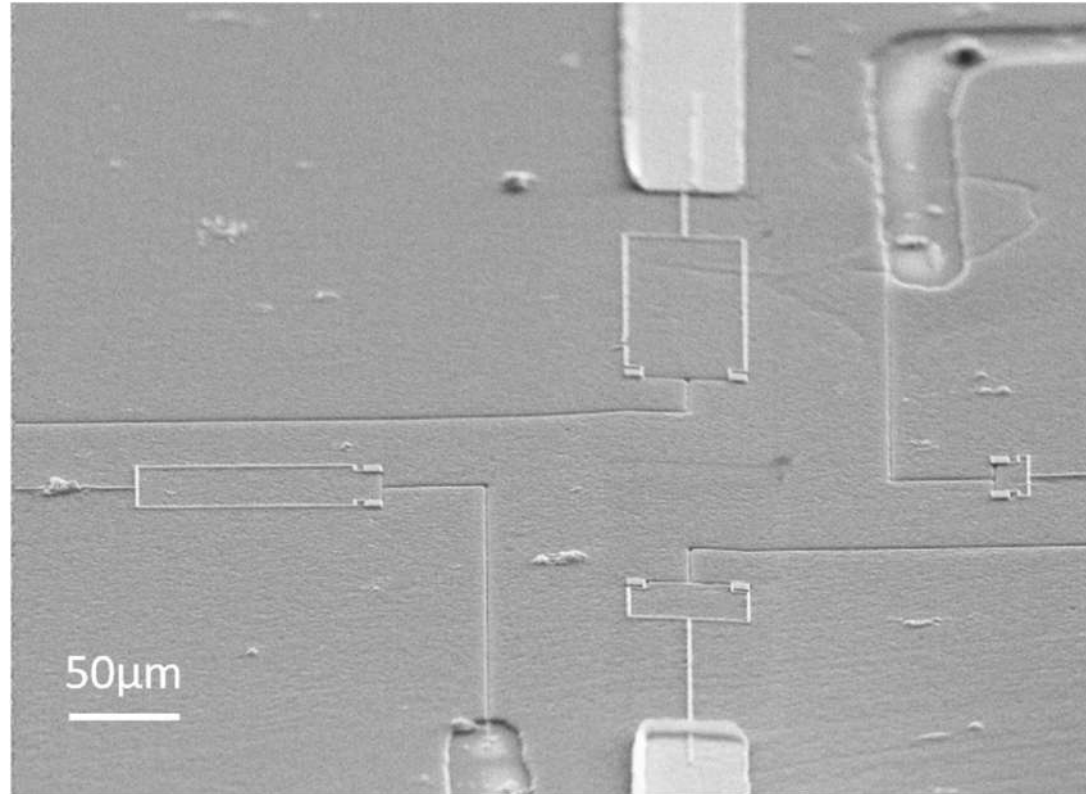
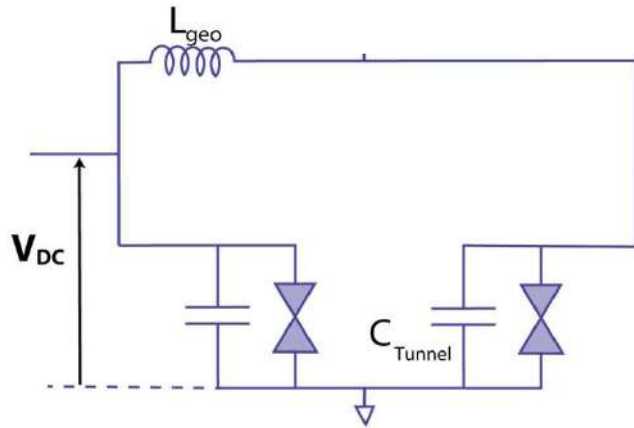
Rediscovering the composition law $C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$



Optimizing the ohmic loss



Towards experimental realizations... stay tuned!



Thank You ! Questions ?

Funding



Djamal Gacemi

M. Jeannin, A. Vasanelli, C. Sirtori



Epitaxial growth

*L. H. Li, A. G. Davies,
E. H. Linfield*



Hua Li, W. Wan, Z. Zhang
Key Laboratory of
Terahertz Solid State Technology,
Shanghai Institute of Microsystem and
Information Technology, Chinese Academy of
Sciences

I. Sagnes



Paris Centre clean room consortium

Spectroscopy

*R. Perreti,
IEMN Lille,
France*



D. But, W. Knap, et al.
Centra,
Warsaw



B. Fix and
P. Bouchon



cmQED team

*C. Feuillet-Palma,
A. Jouan*

